

# Efficient Multi-Modal Route Planning

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Master Thesis

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Albert-Ludwigs-Universität Freiburg



**UNI  
FREIBURG**



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  - more than one solution (bi-criteria optimization)
    - minimize travel time & # transfers + [walking between stations]

# Overview



- Constructing Transit & Road Network
- Combining Road & Transit Network
- Bi-criteria Optimization
- Experiments
- Conclusion

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- Time-Expanded vs. Time-Dependent Approach

# Time-Expanded Network



- One node per arrival & departure event

station	time
A	10:00 (dep)
B	10:28 (arr) 10:28 (dep)
C	10:55 (arr)

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station	time
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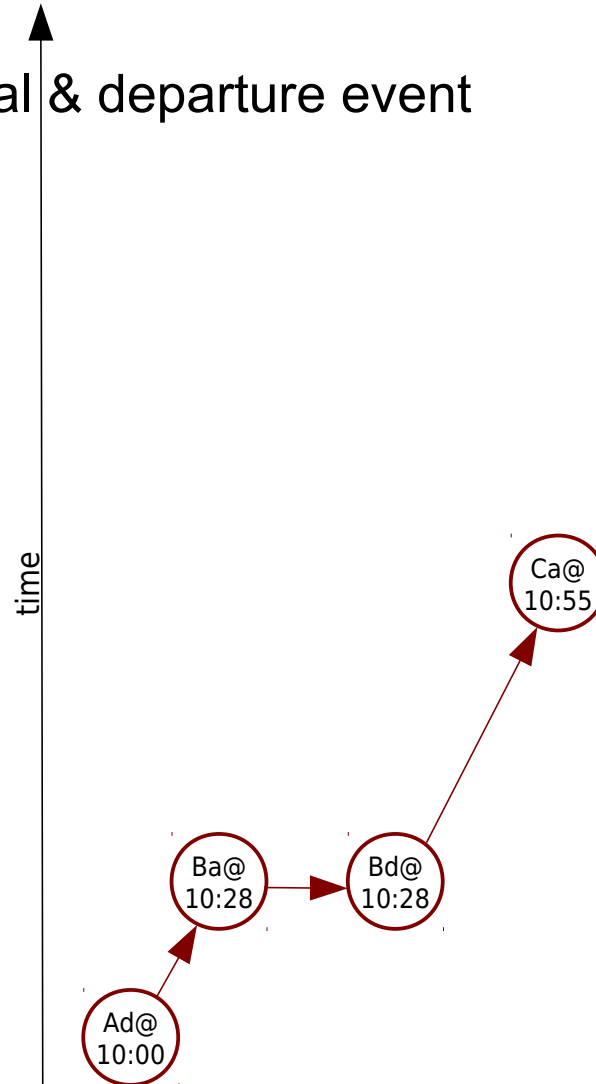
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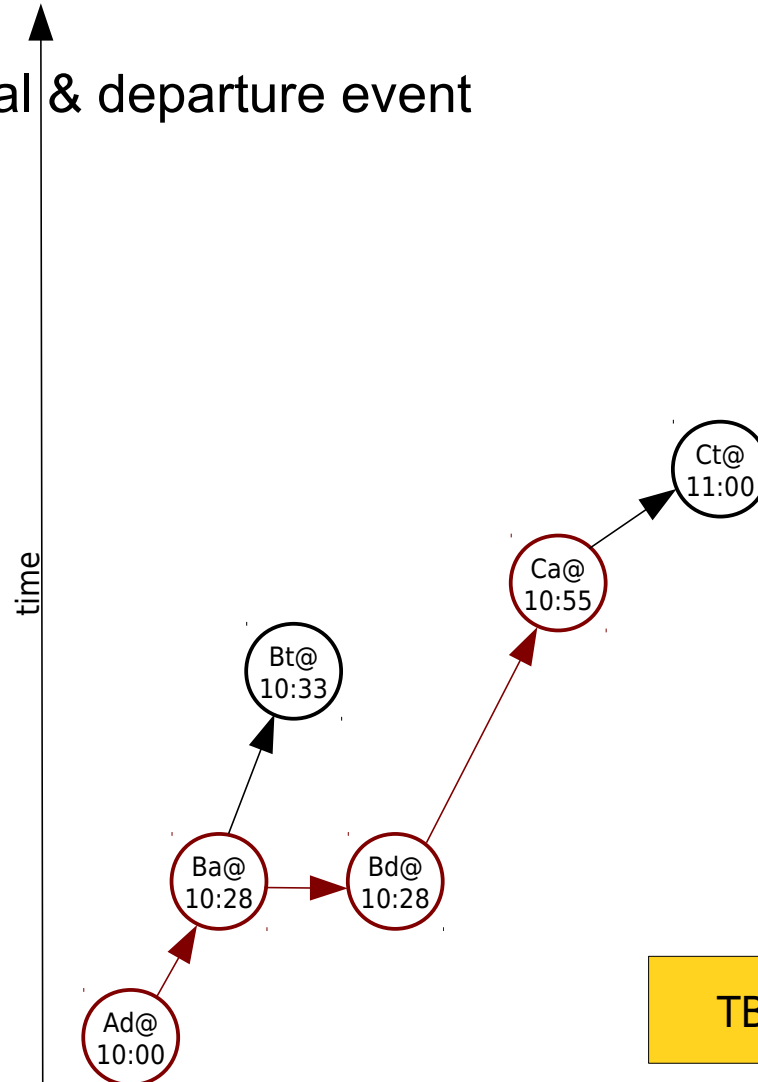
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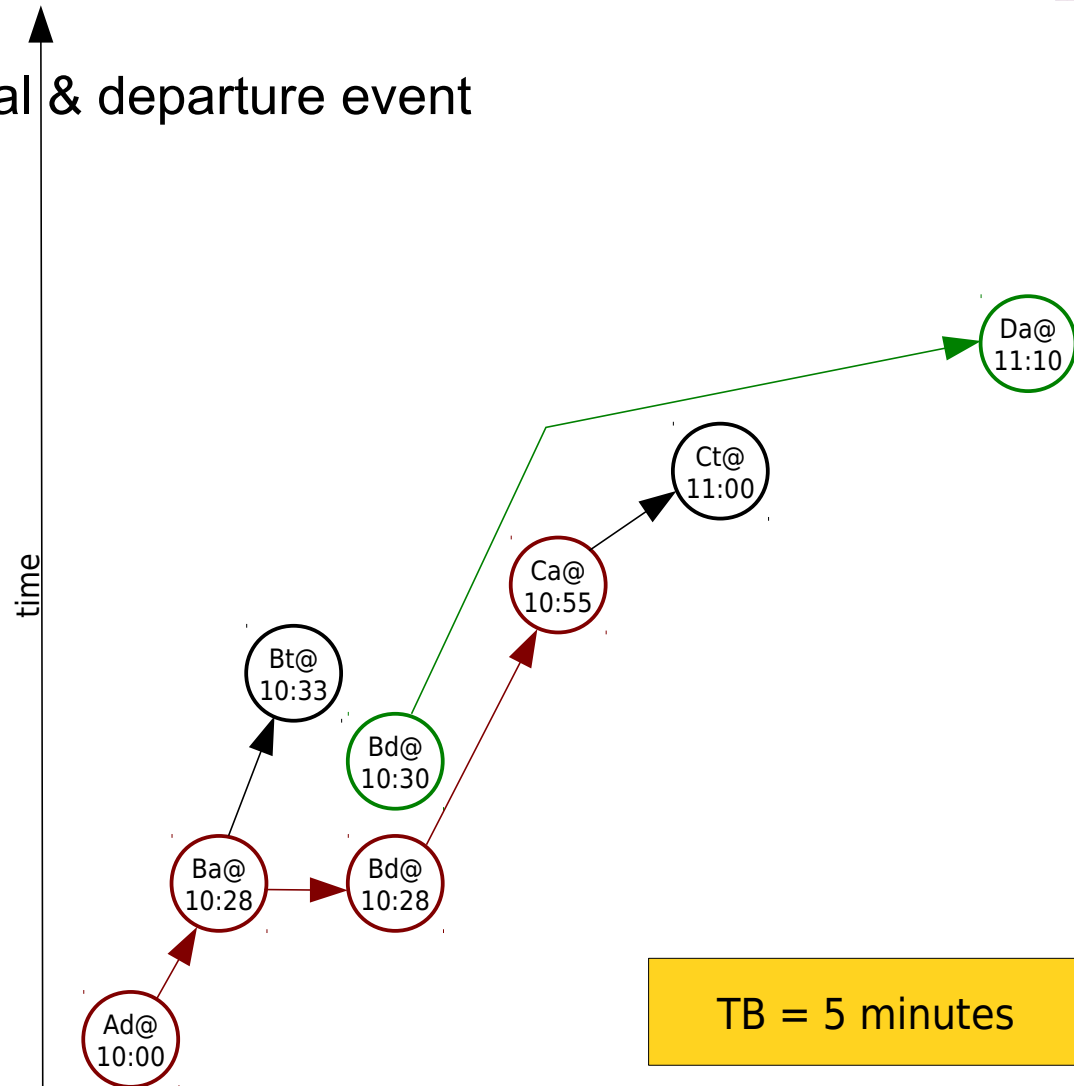
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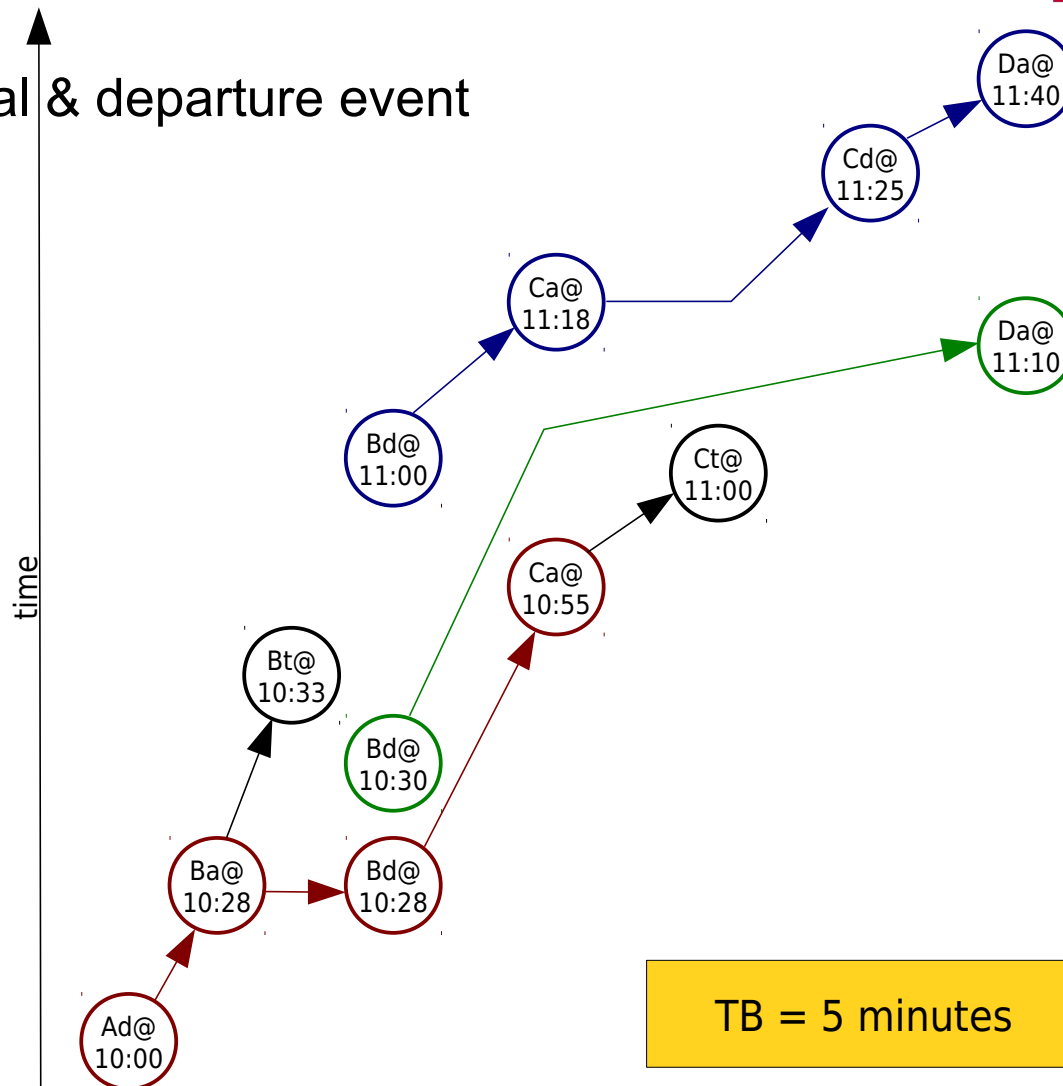
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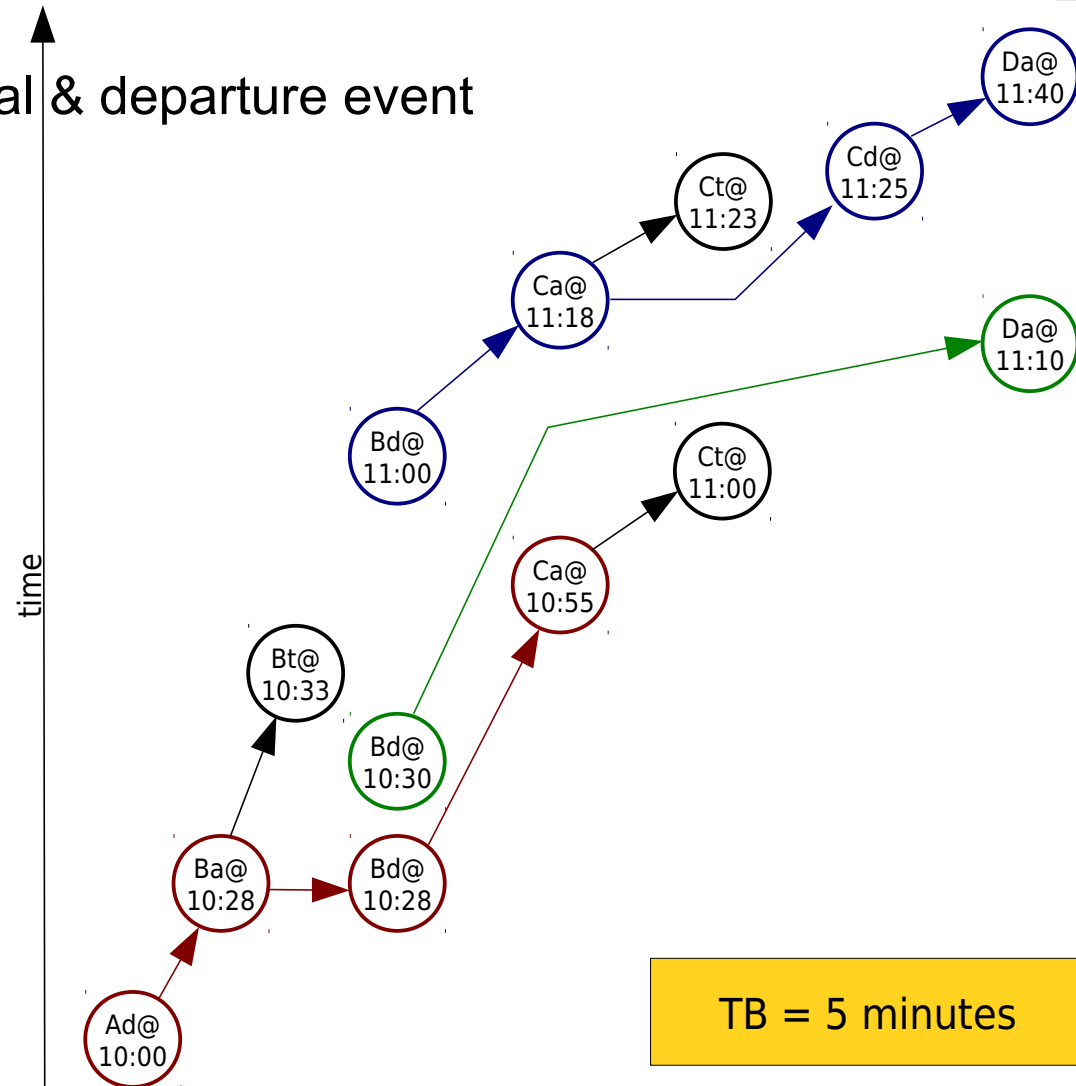
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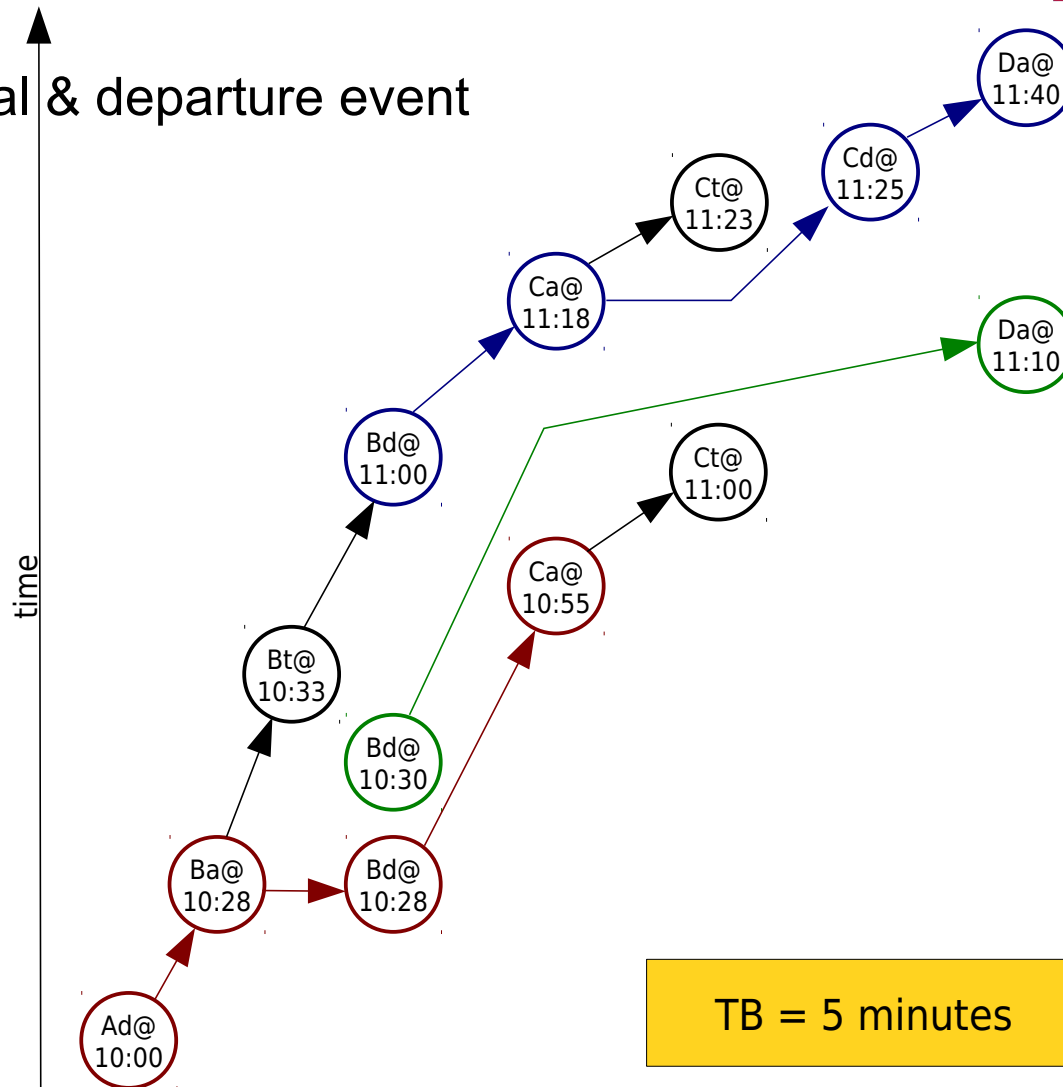
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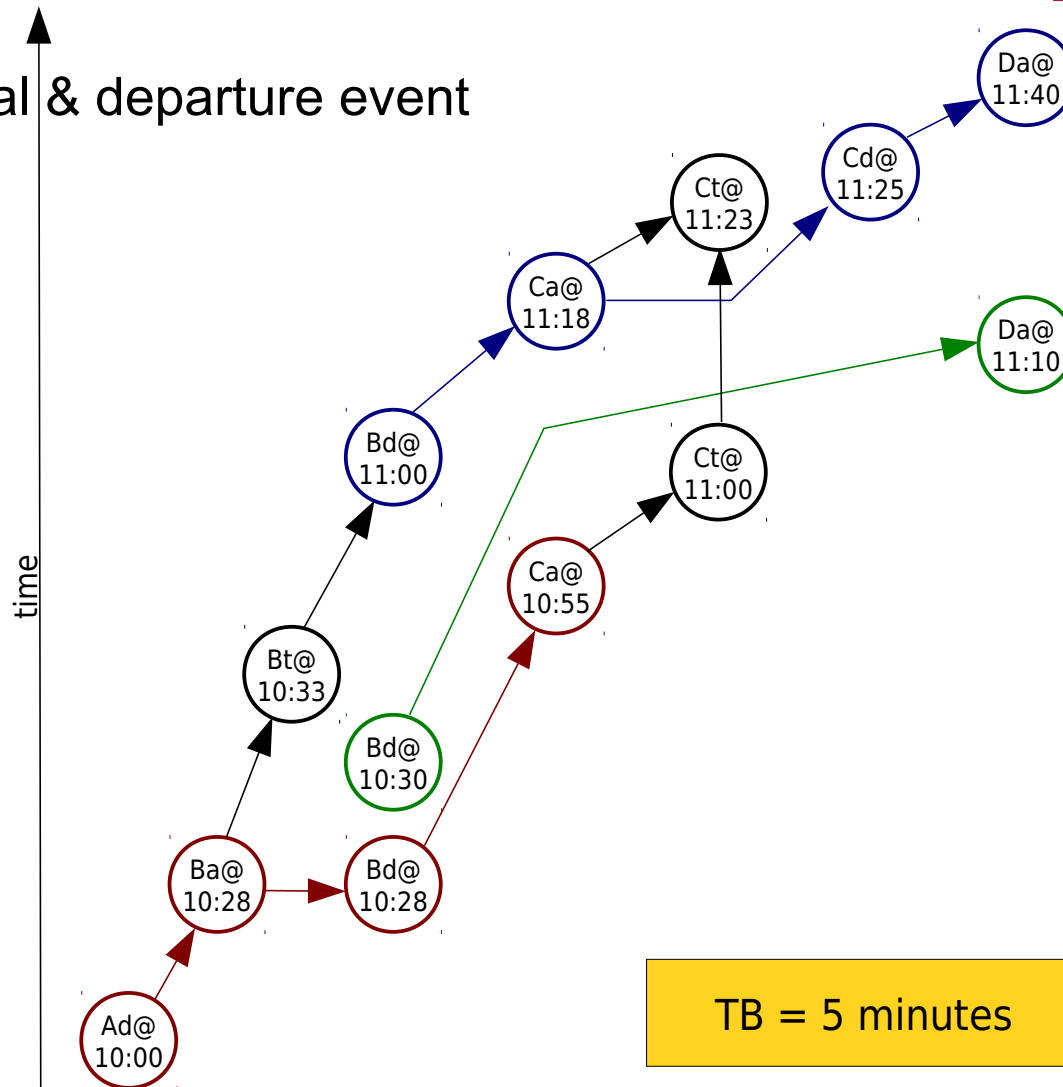
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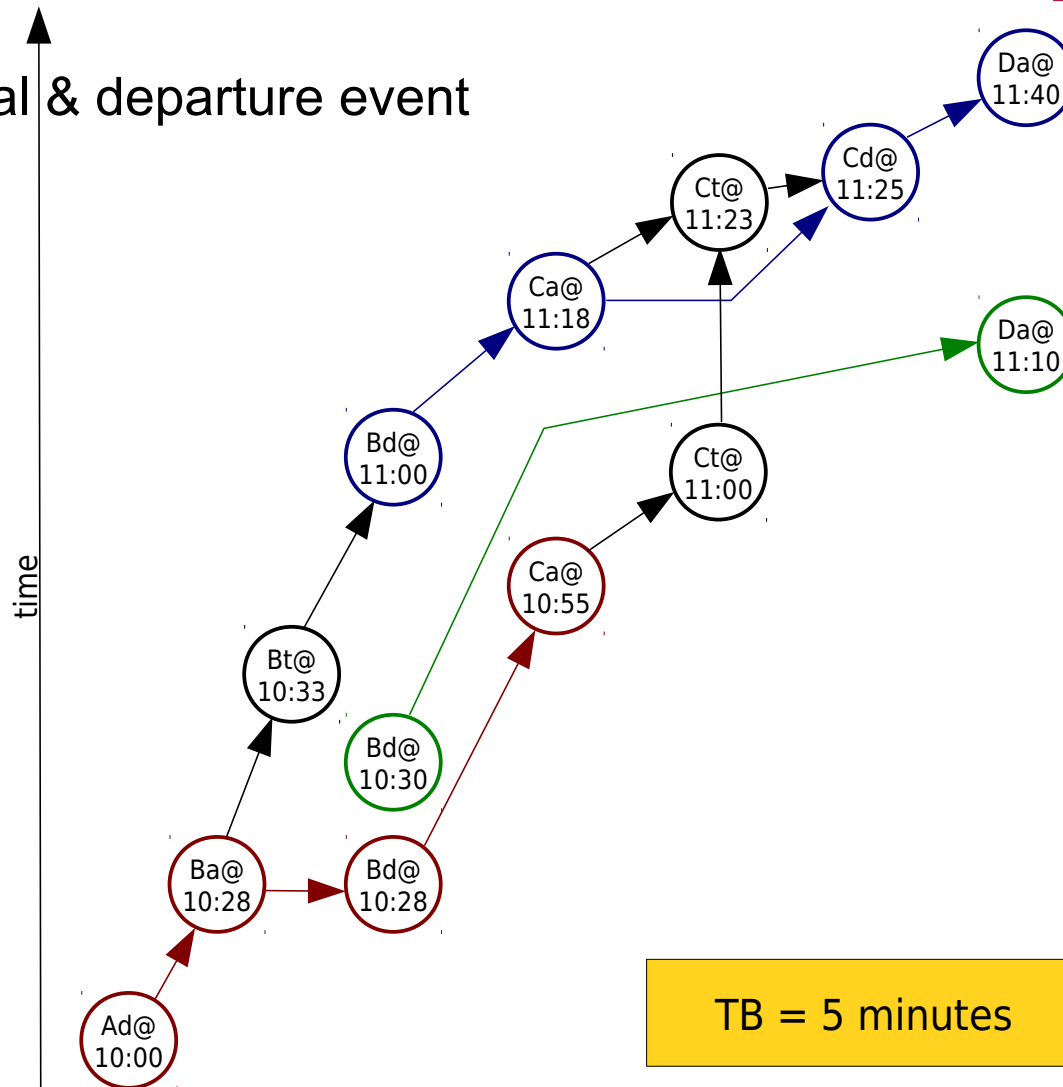
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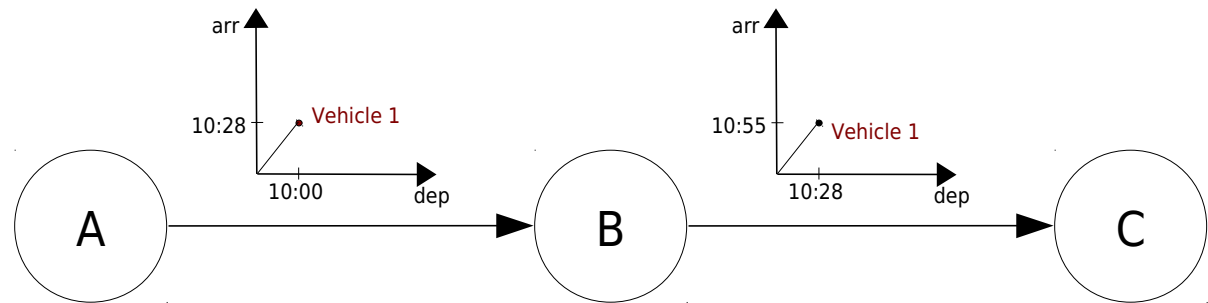
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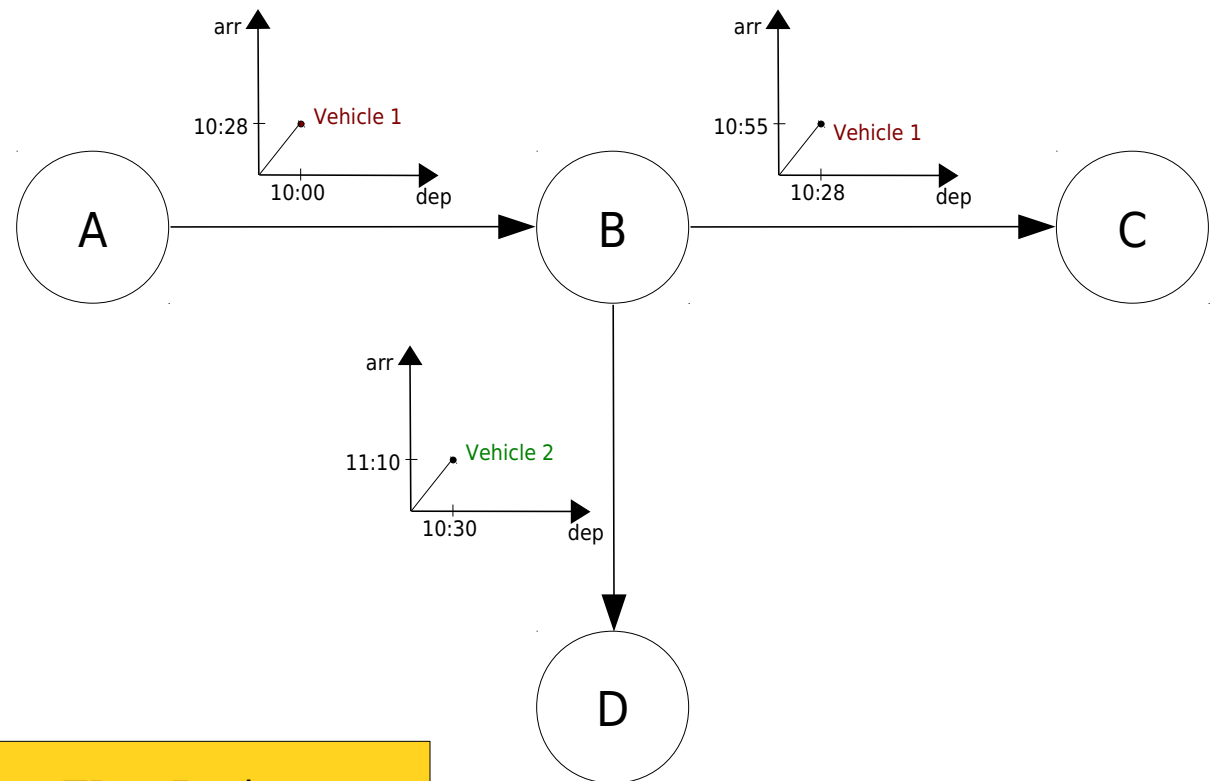
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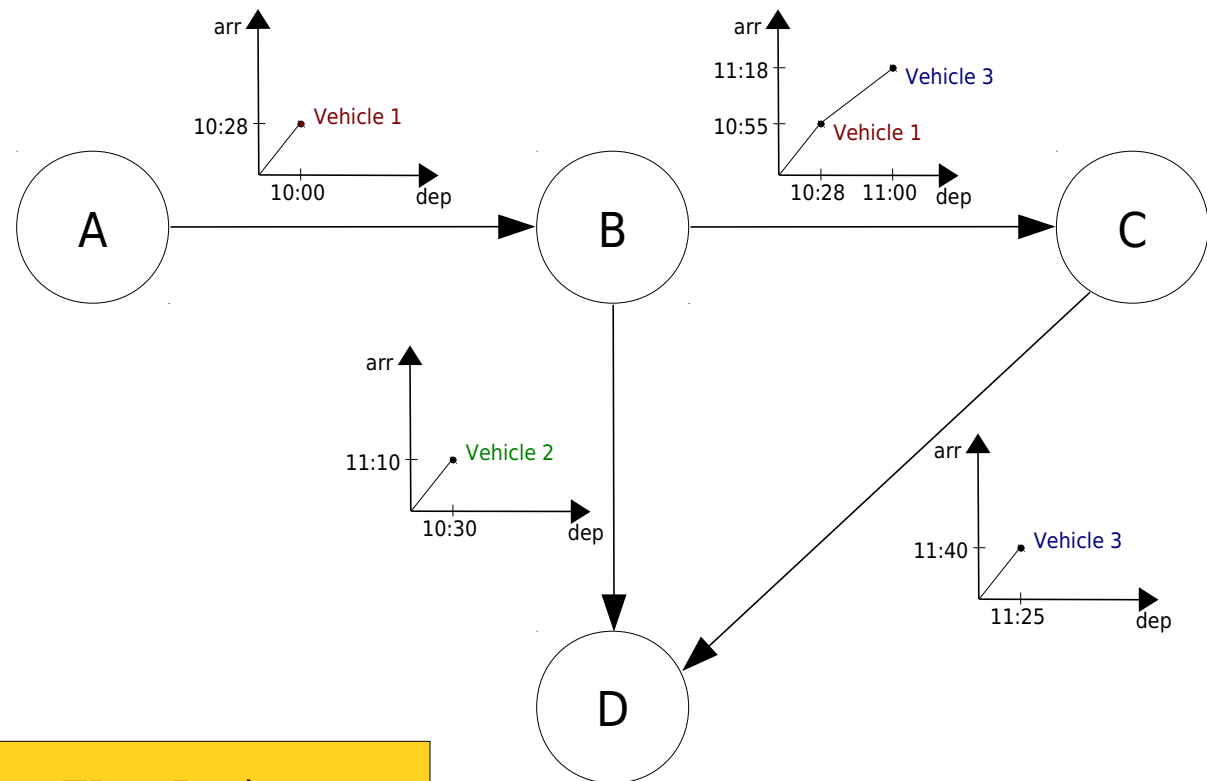
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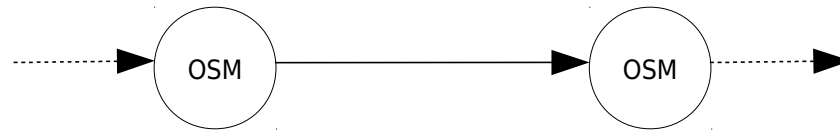
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- Data: OSM (OpenStreetMaps)
  - ways (street as vector of nodes)
  - nodes with latitude and longitude

# Combining Road & Transit Network

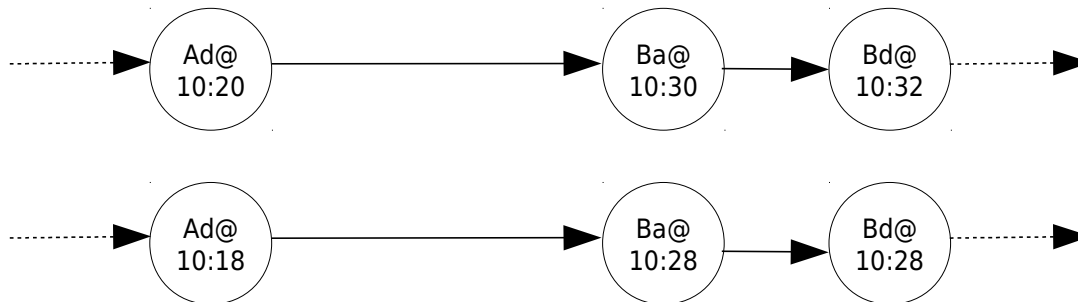


- Time-Expanded Network

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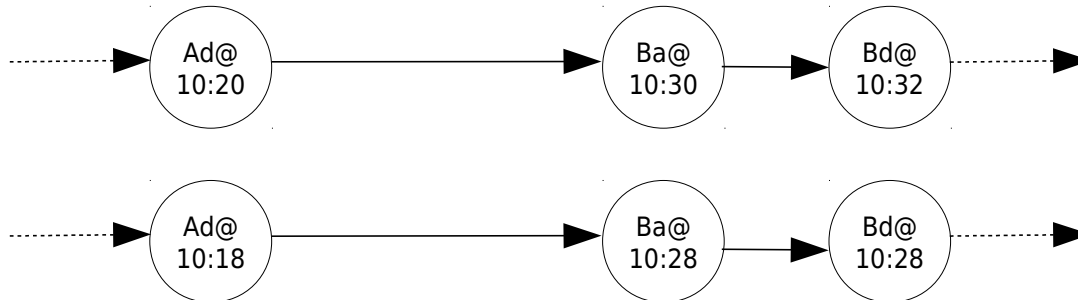


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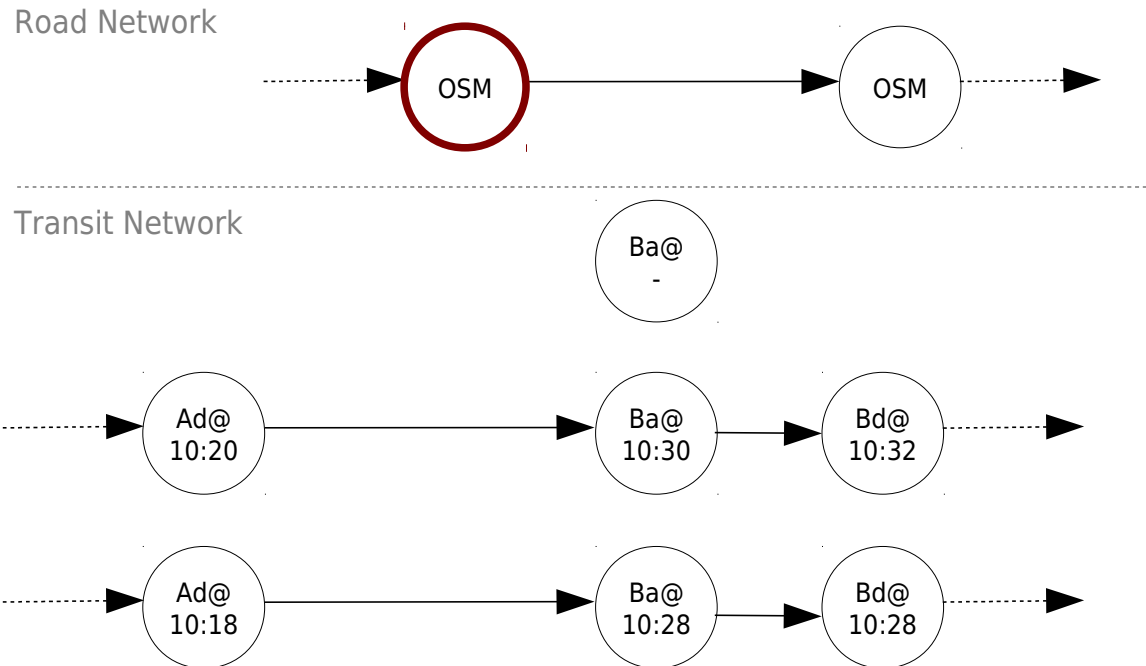




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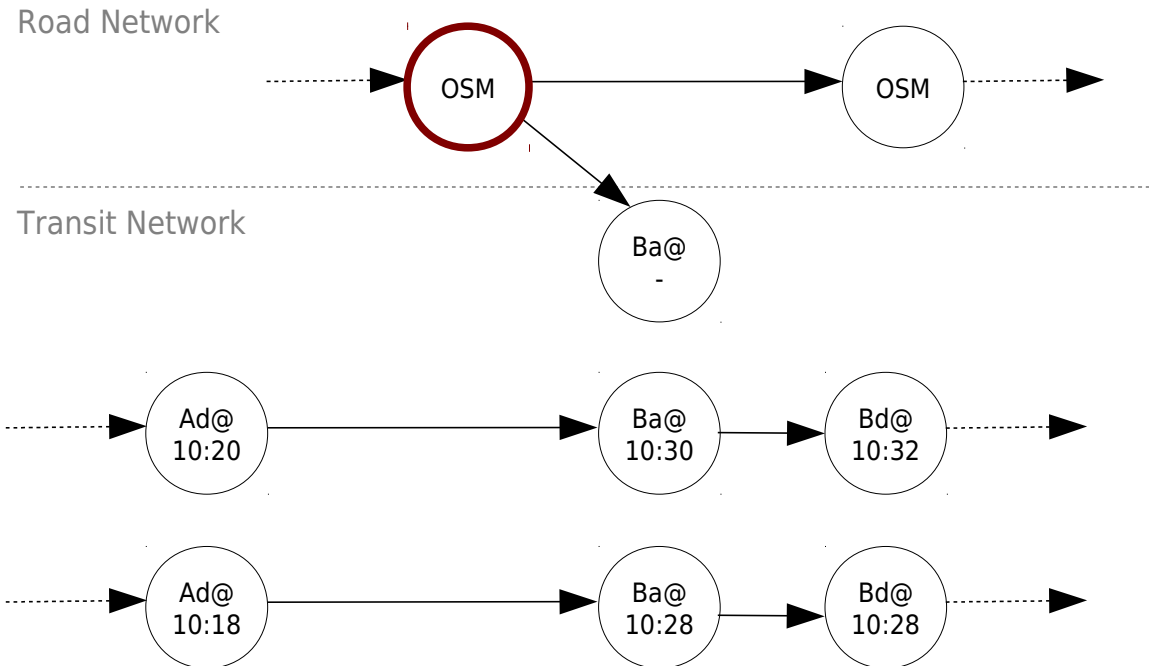
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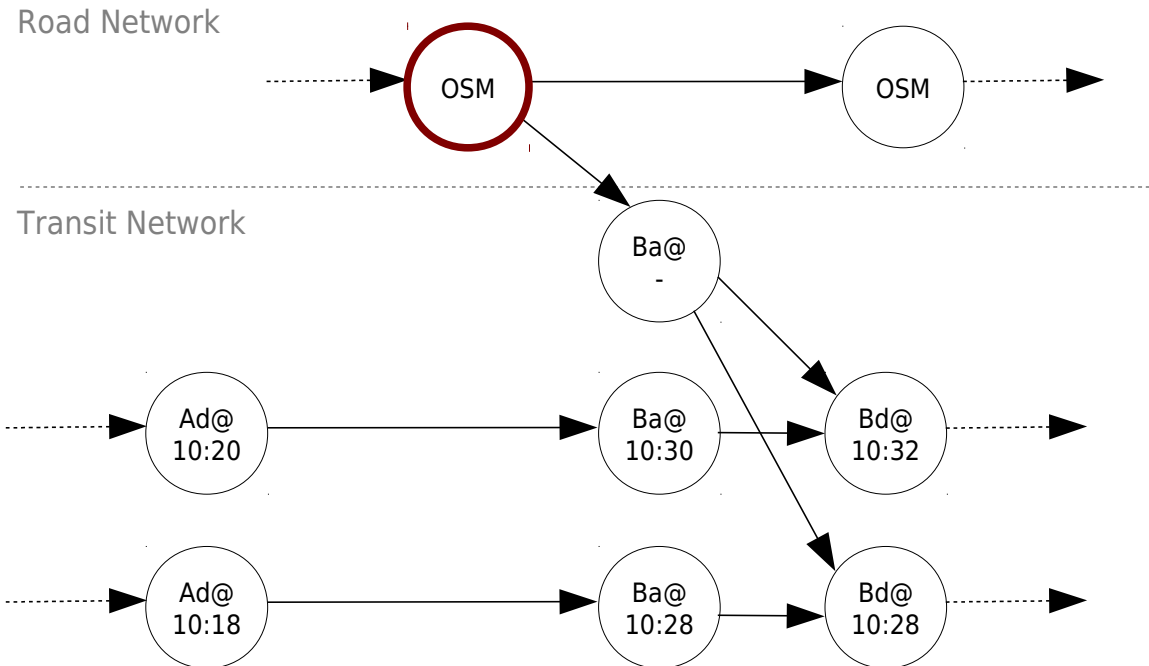
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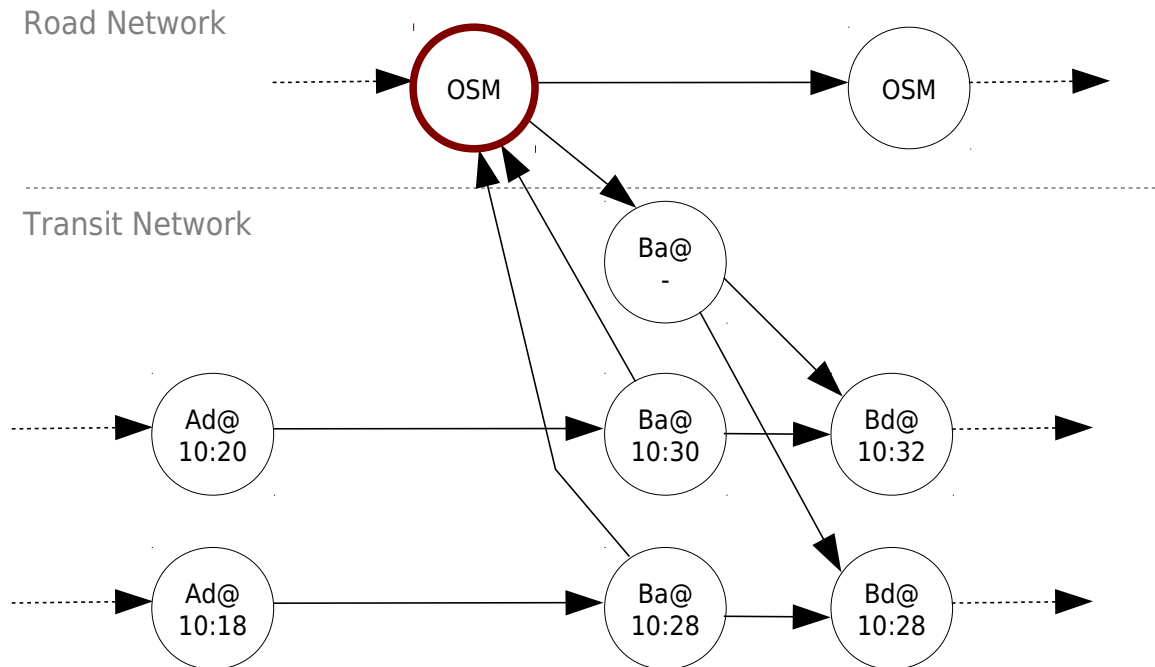
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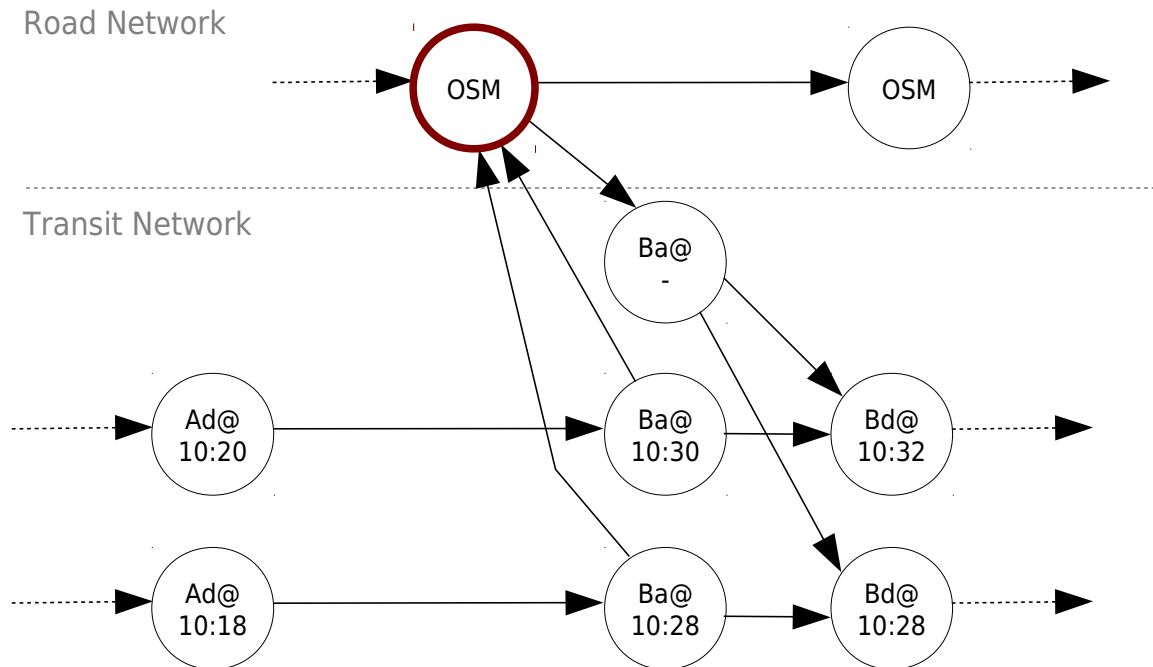
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# Combining Road & Transit Network



## Time-Expanded Network



## Time-Dependent Network

- adding bidirectional edge from the geographically closest OSM node to the corresponding station

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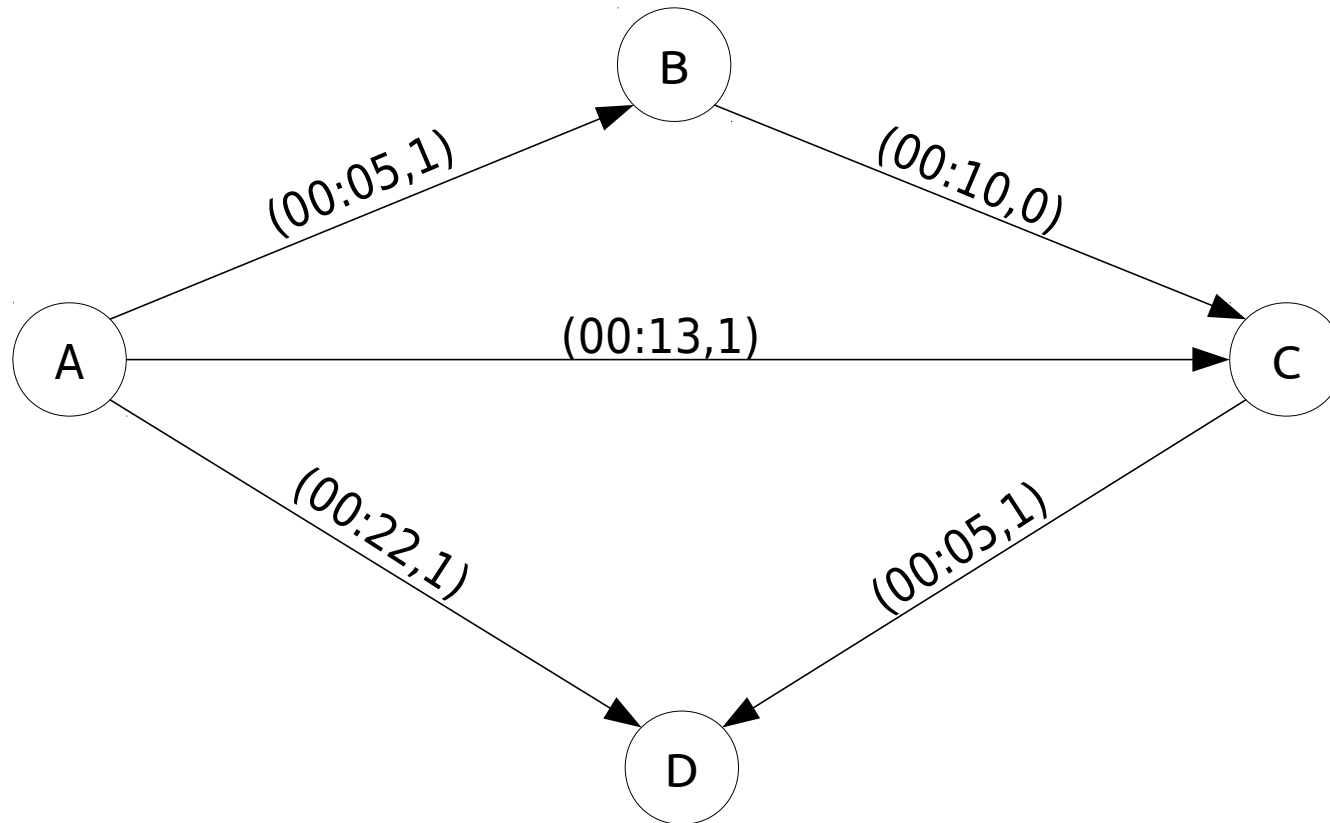
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  - compute all optimal solutions
    - use a Multi Label Dijkstra

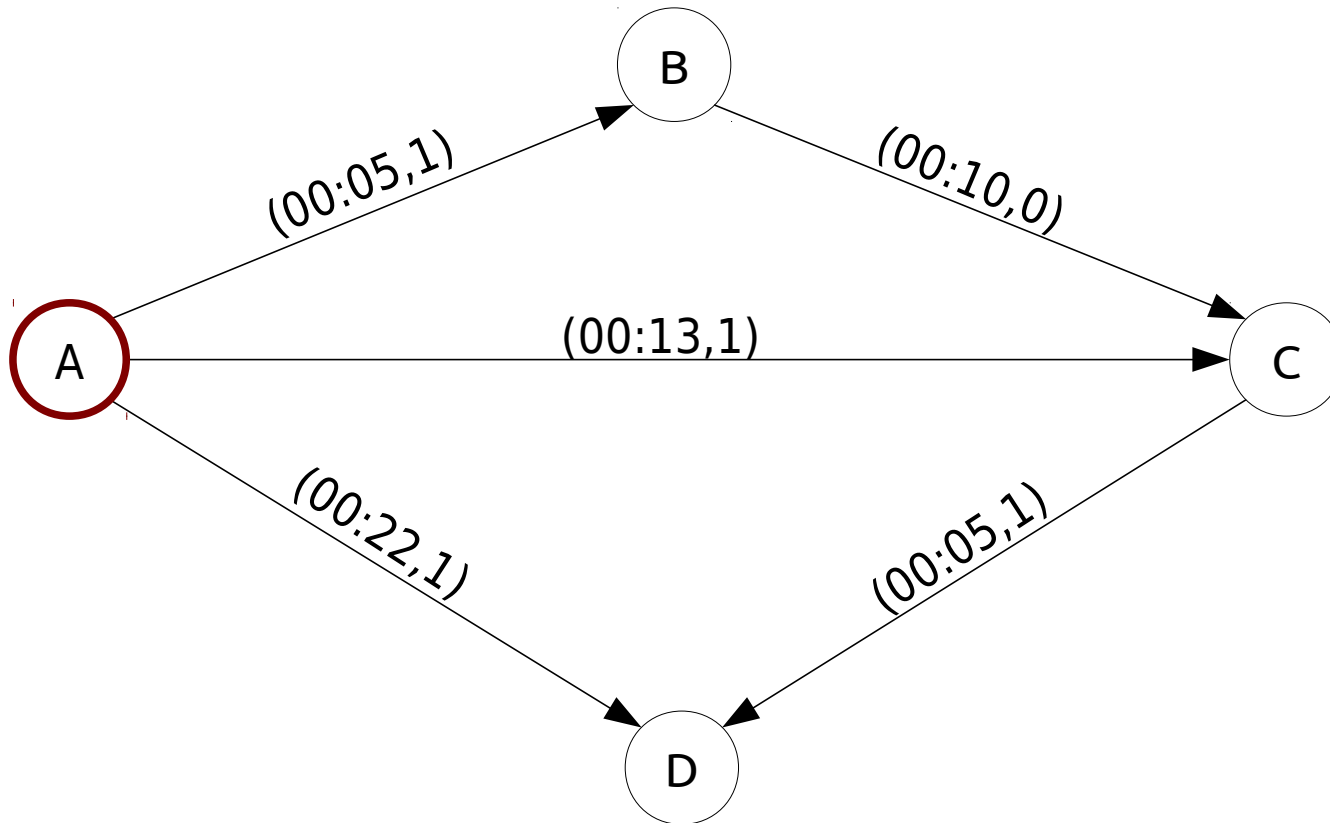
- Example execution



# Multi Label Dijkstra



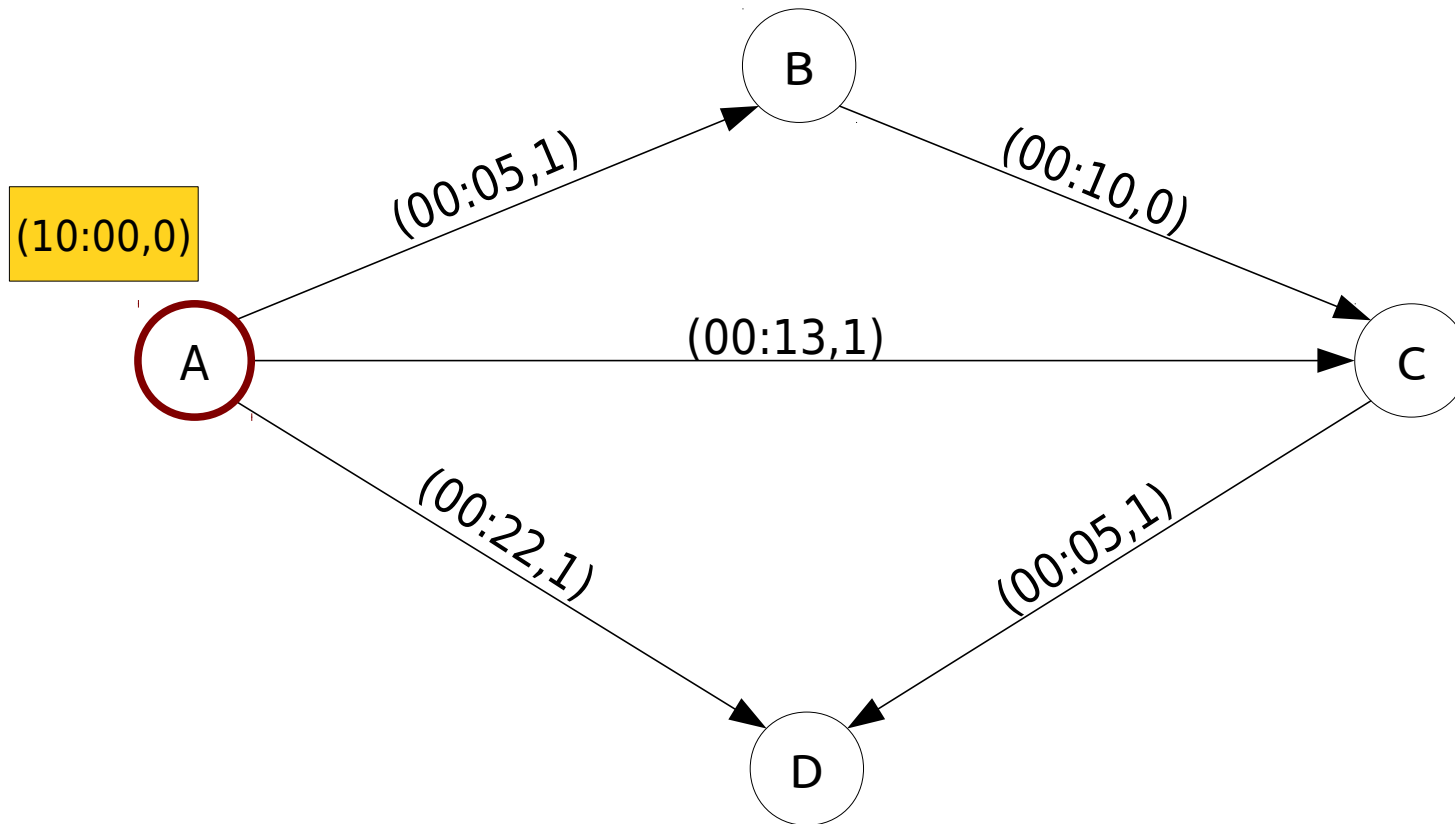
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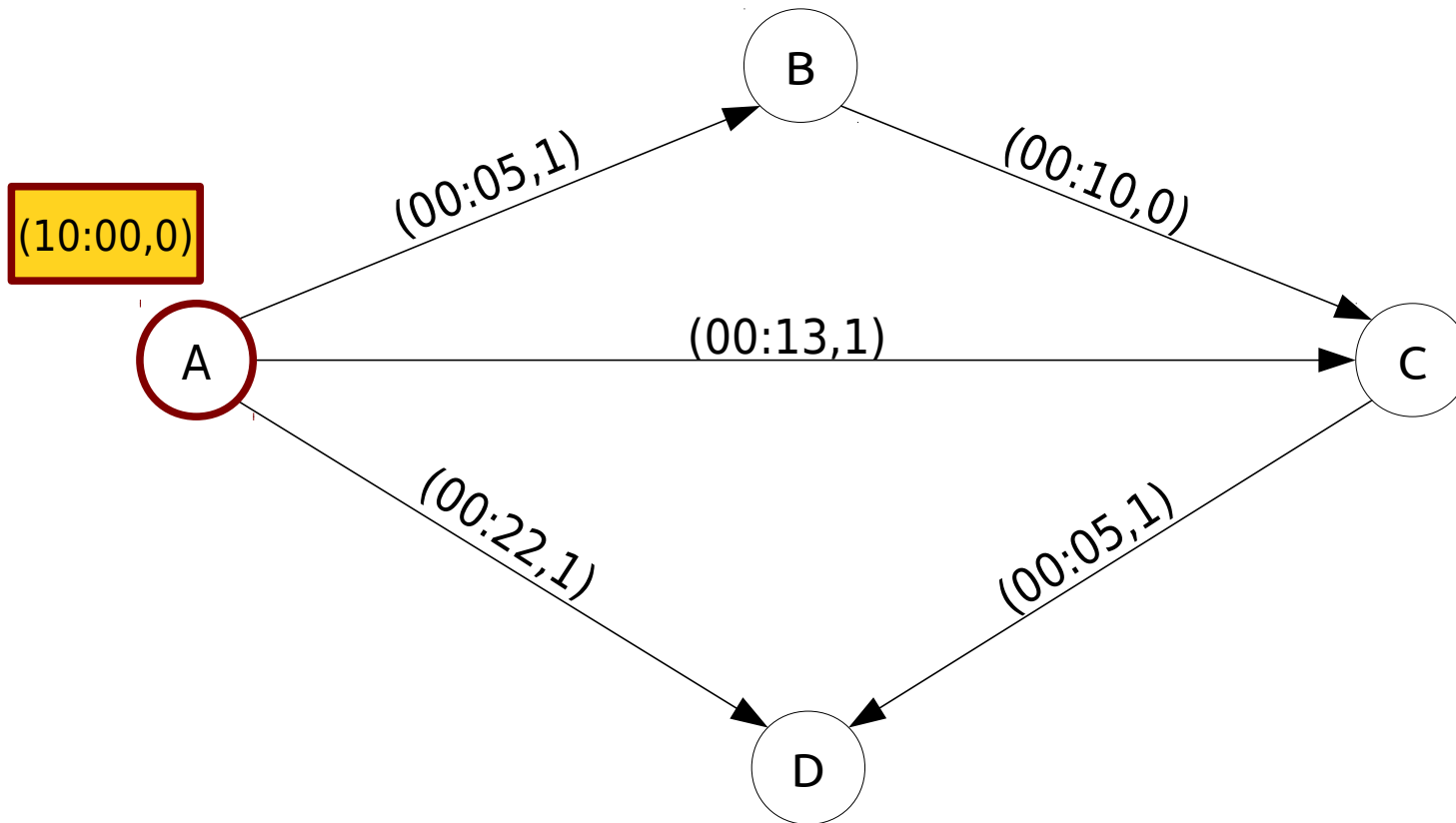
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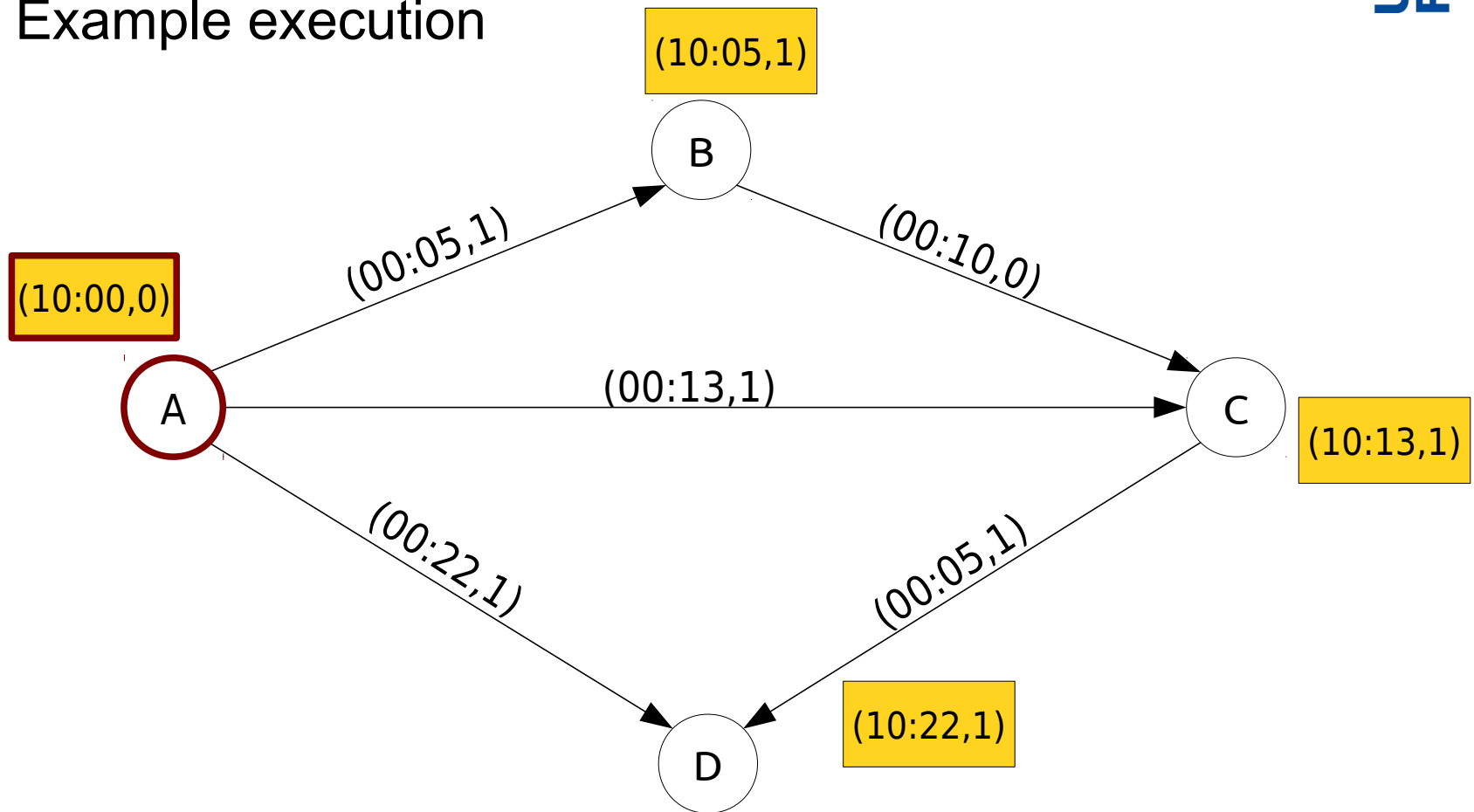




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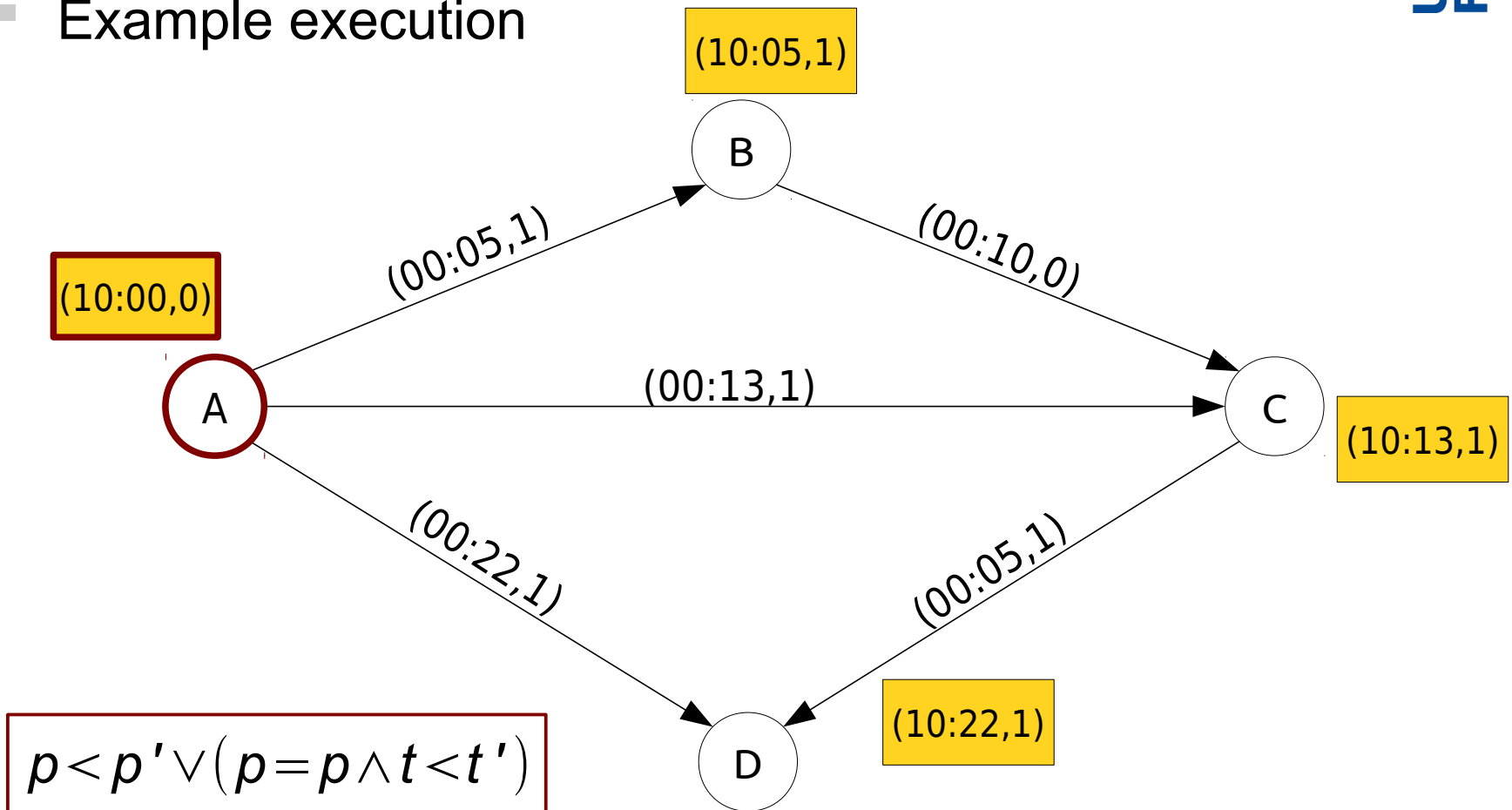
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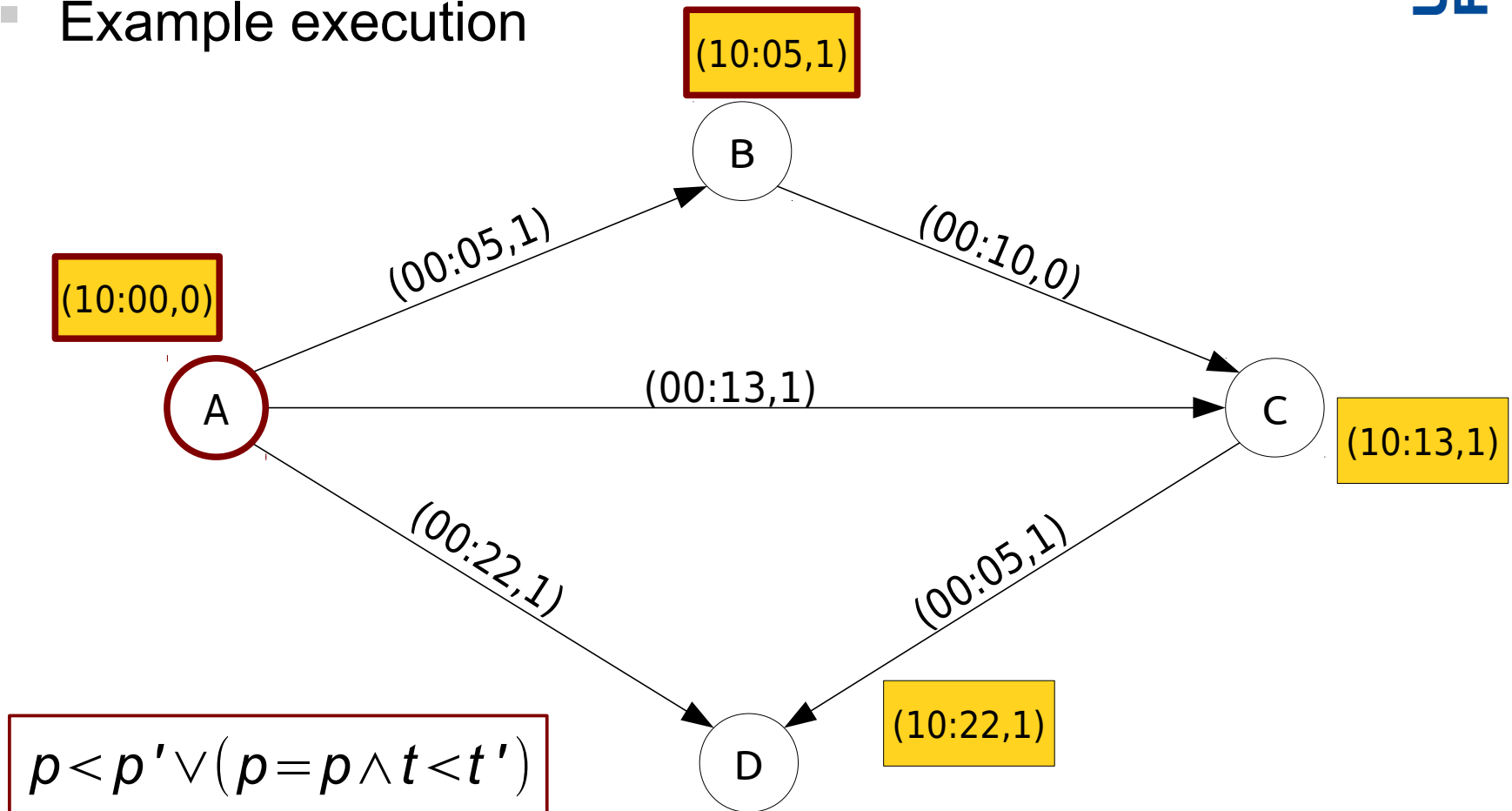
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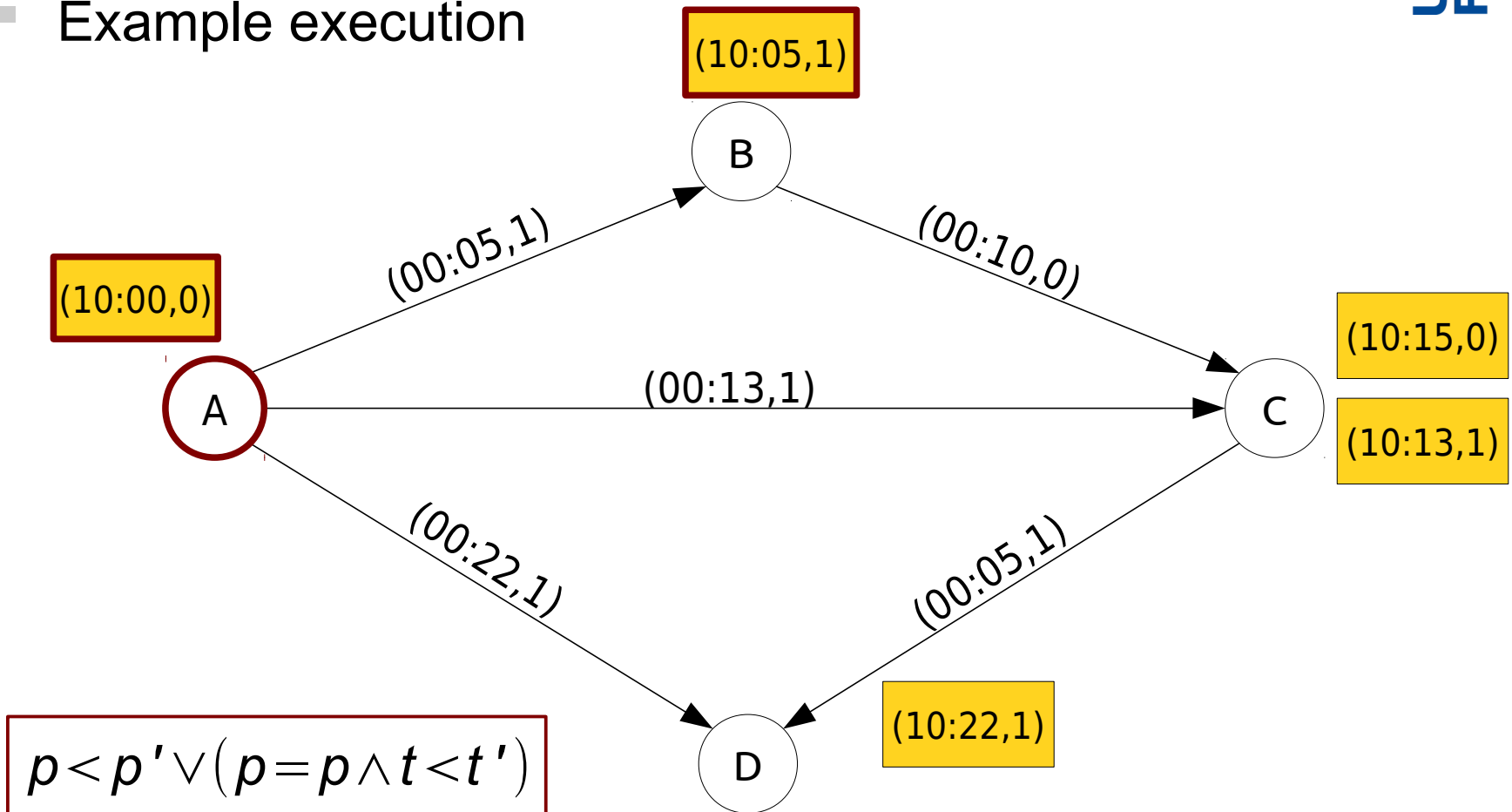
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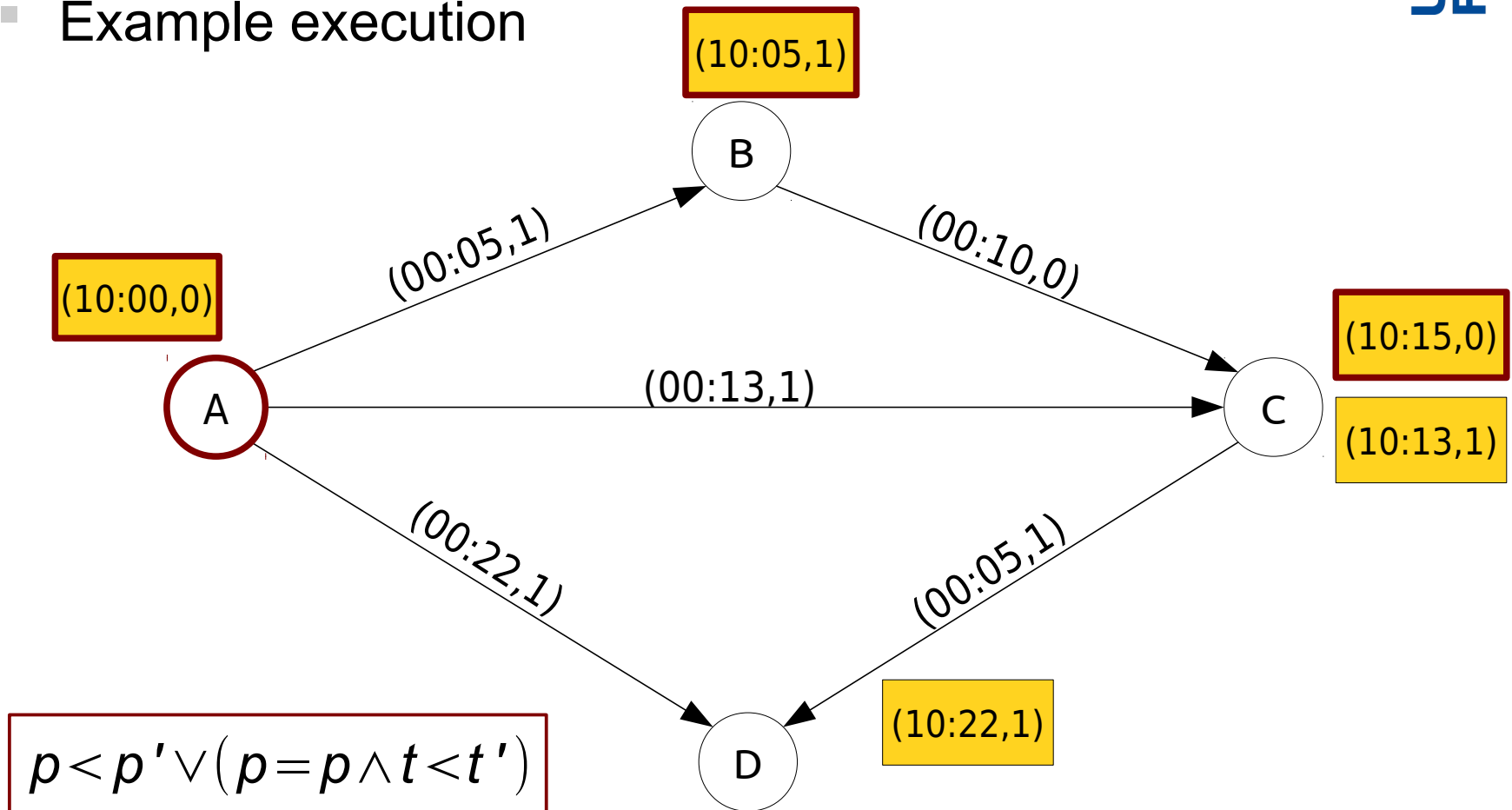
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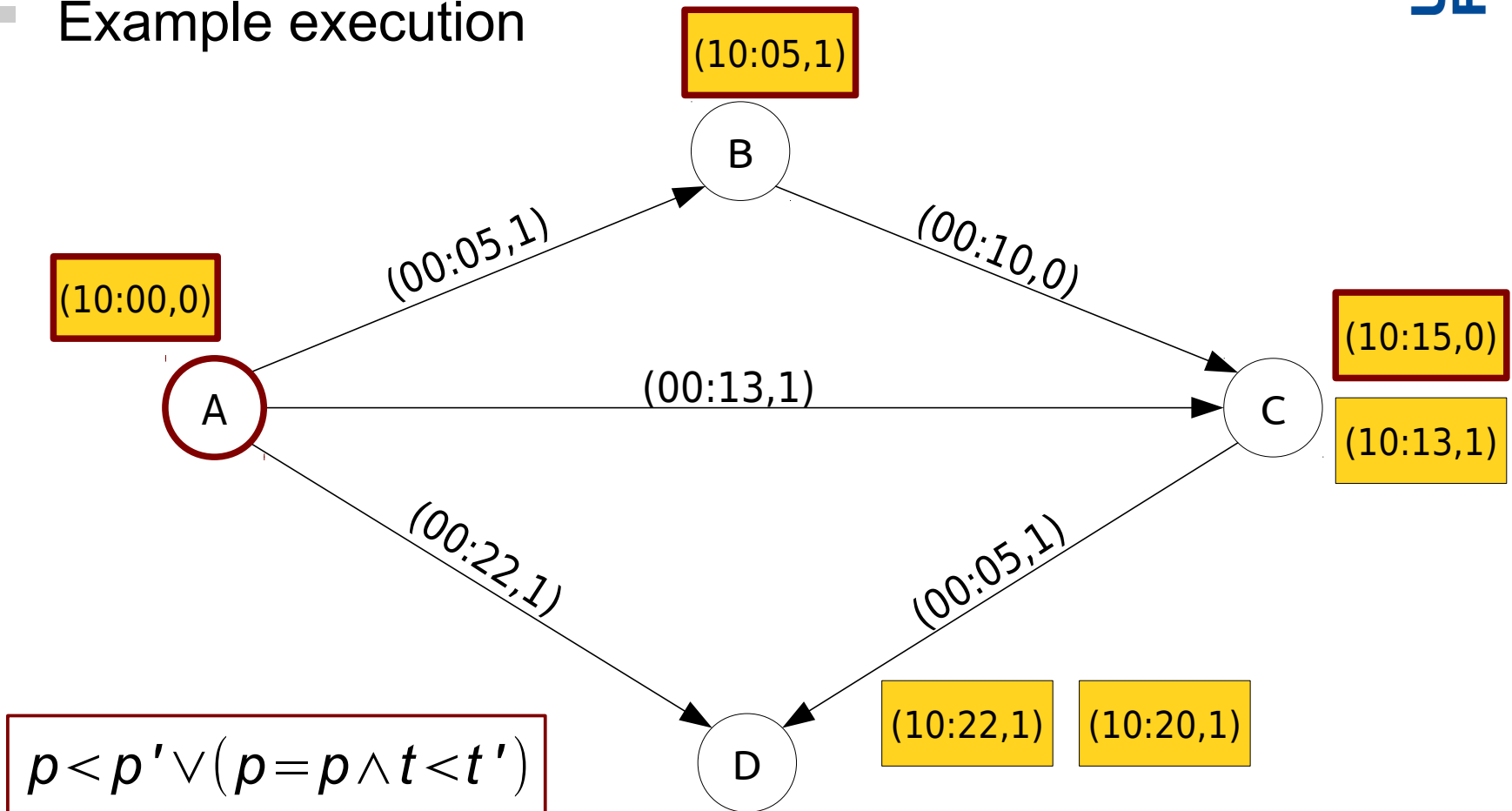
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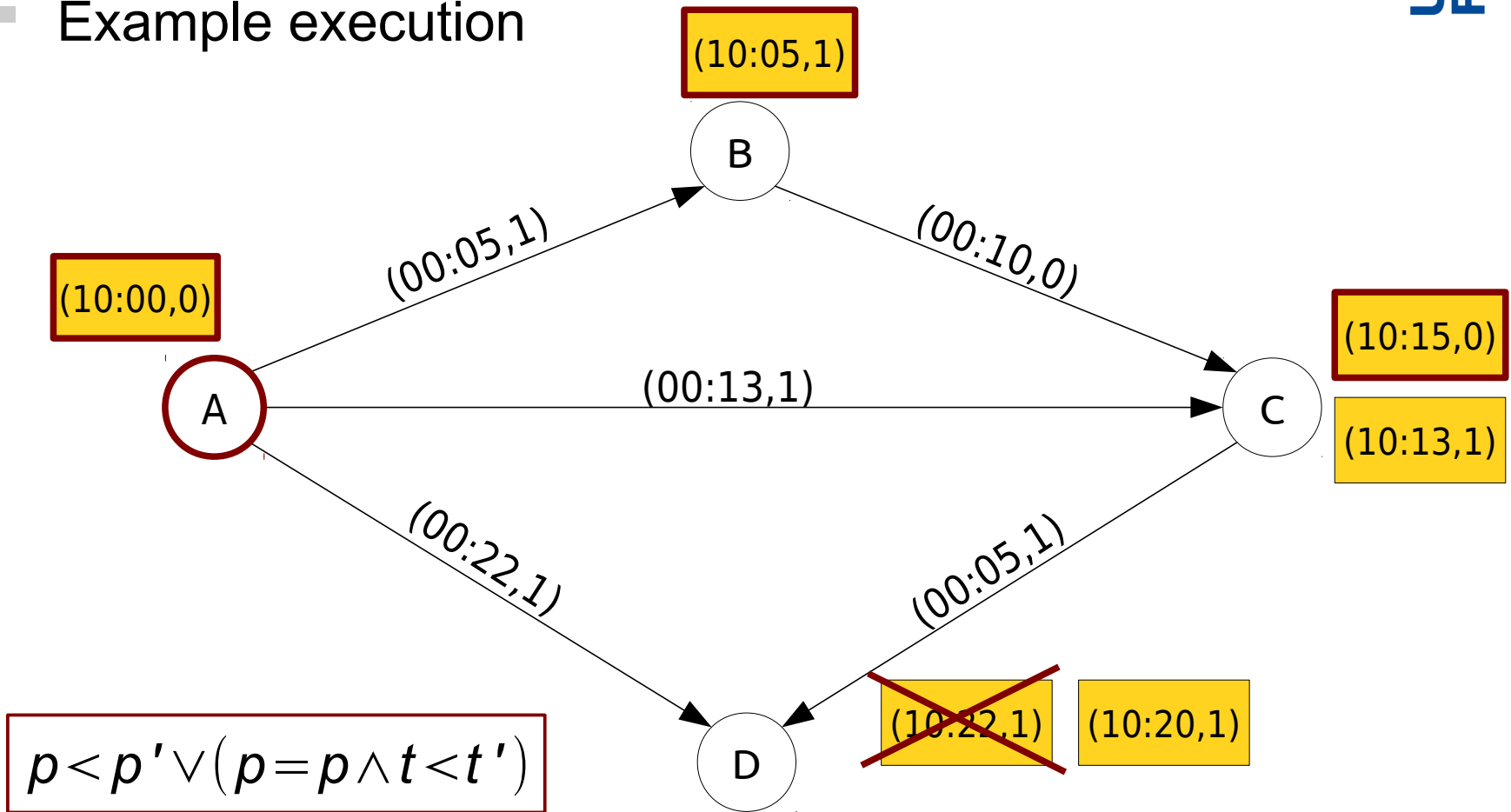
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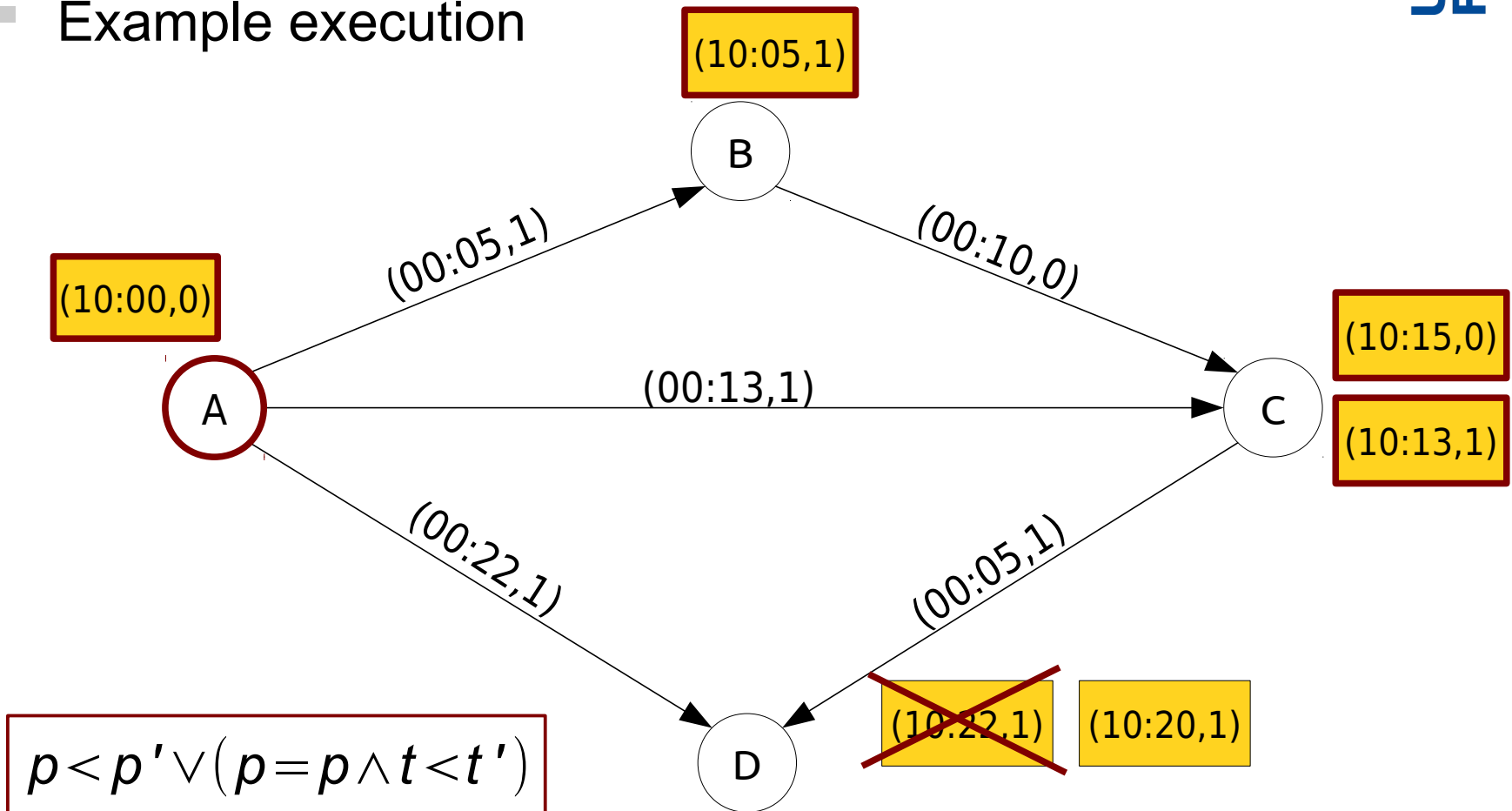
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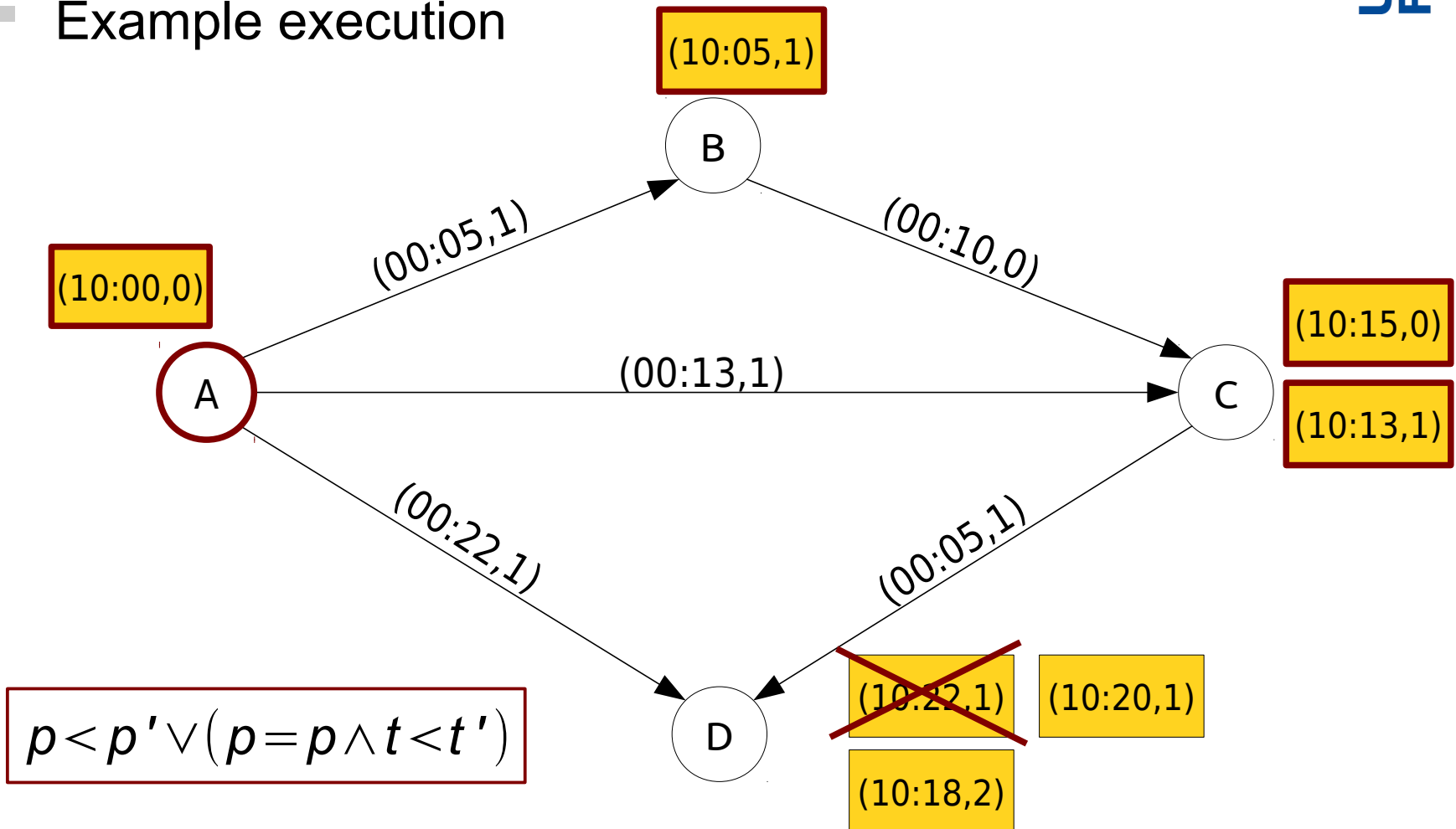




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- If  $(t,p)_w$  is not dominated or incomparable to all  $(t',p')_w$ 
  - insert  $(t,p)_w$  into label set at  $w$
  - insert  $(t,p)_w$  into priority queue

- Comparing the Graph Size

	# nodes	# edges	space
Exp	48.3 M	112.4 M	10 679 MB
Dep	4.5 M	9.4 M	1 643 MB

- GTFS Data: New York City Subway, New York City Bus (Bronx, Brooklyn, Manhattan, Queens, Staten Island), Long Island Bus and the Metro-North Railroad
- OSM Data: State New York
- Date interval: 09.04.2012 – 15.04.2012

- Comparing Performance

	time	settled labels	labels/station
bi-criteria (# transfers only)			
Exp	62.3 s	20.7 M	-
Dep	16.7 s	2.0 M	3
bi-criteria (# transfers and minimizing walking)			
Exp	89.2 s	33.8 M	-
Dep	58.6 s	2.4 M	13

- 1000 random paths

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- Minimize travel time & # transfers + [walking between stations]
- TD approach about 3.7 times faster in average than the TE approach (bi-criteria)
- When minimizing walking between stations in addition, the gap is smaller (speed up 1.5)



- Interval e. g. 09.04.2012, 00:00 – 15.04.2012, 24:00
- Have connection between stations/nodes for a day if there is a valid connection between stations
- Times stored are integers relative to the begin of the interval
  - e. g. 11.04.2012,10:20:
    - $t = 2 \cdot 24 \cdot 3600 + 10 \cdot 3600 + 20 \cdot 60$
- Actual time of day =  $t \bmod (24 \cdot 3600)$
- Actual day =  $\lfloor t / (24 \cdot 3600) \rfloor$

# Reducing Labels per Station (TD)

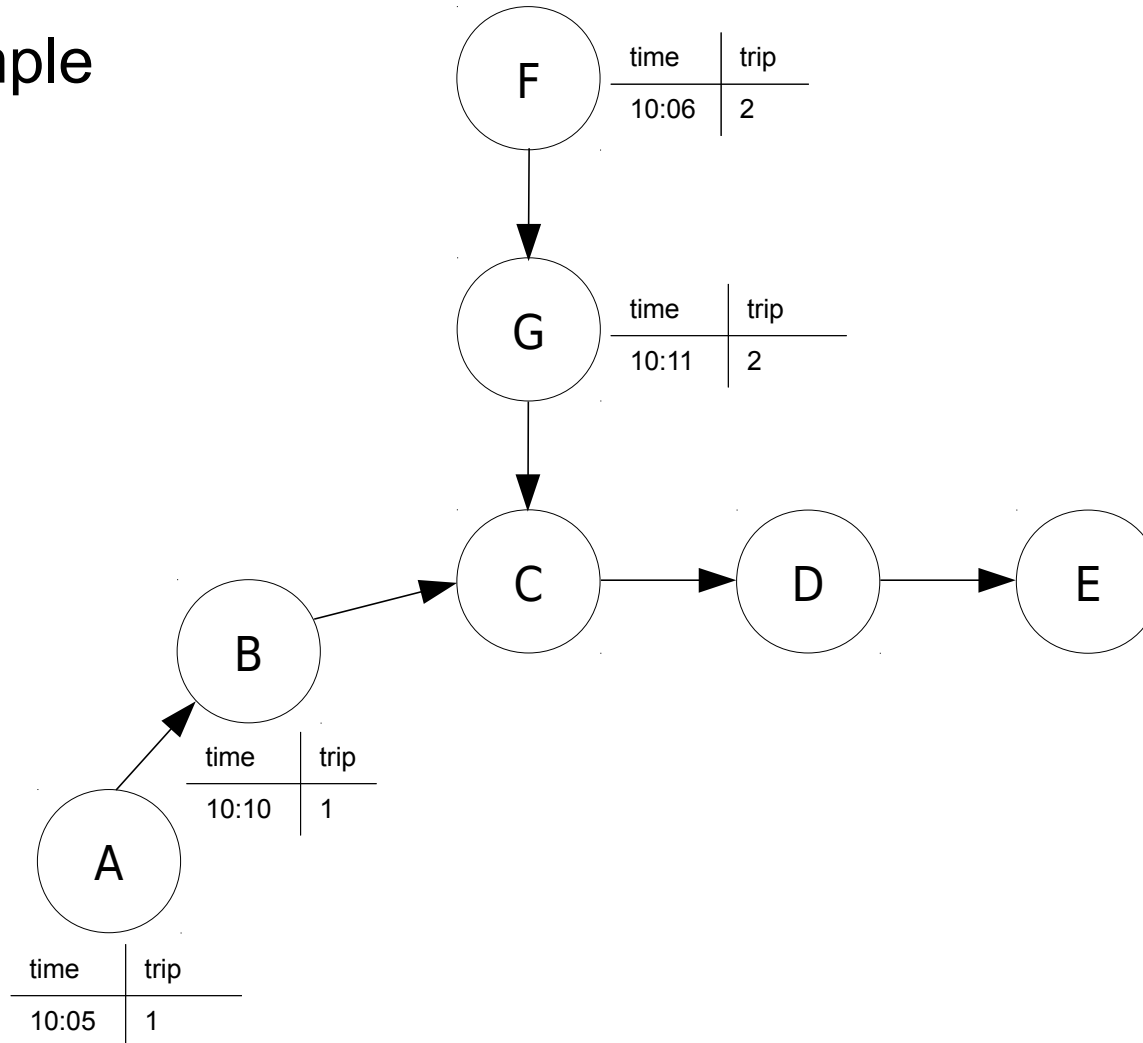


- Problem: too many labels per station
- Solution: for each trip pair remember how many stations both trips have in common up to the final station
- Do precomputation:
  - hash map  $h : (\ell, \ell') \rightarrow (\text{arr}(S, \ell), \text{arr}(S, \ell'))$
  - If for two labels  $(t, p), (t', p')$  there is an entry and  $t \geq \text{arr}(S, \ell) \wedge t' \geq \text{arr}(S, \ell')$ 
    - compare labels in the time-expanded sense

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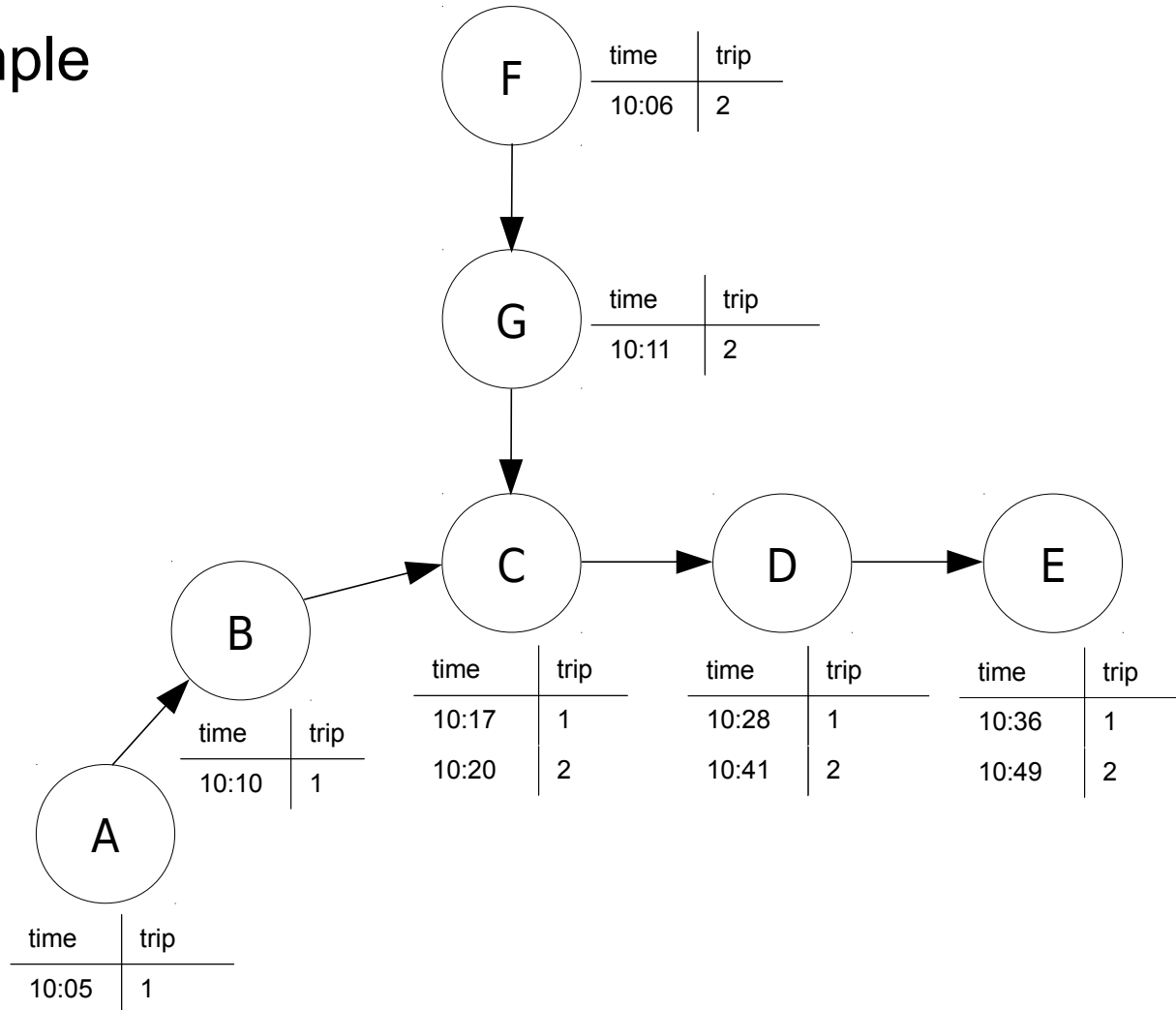
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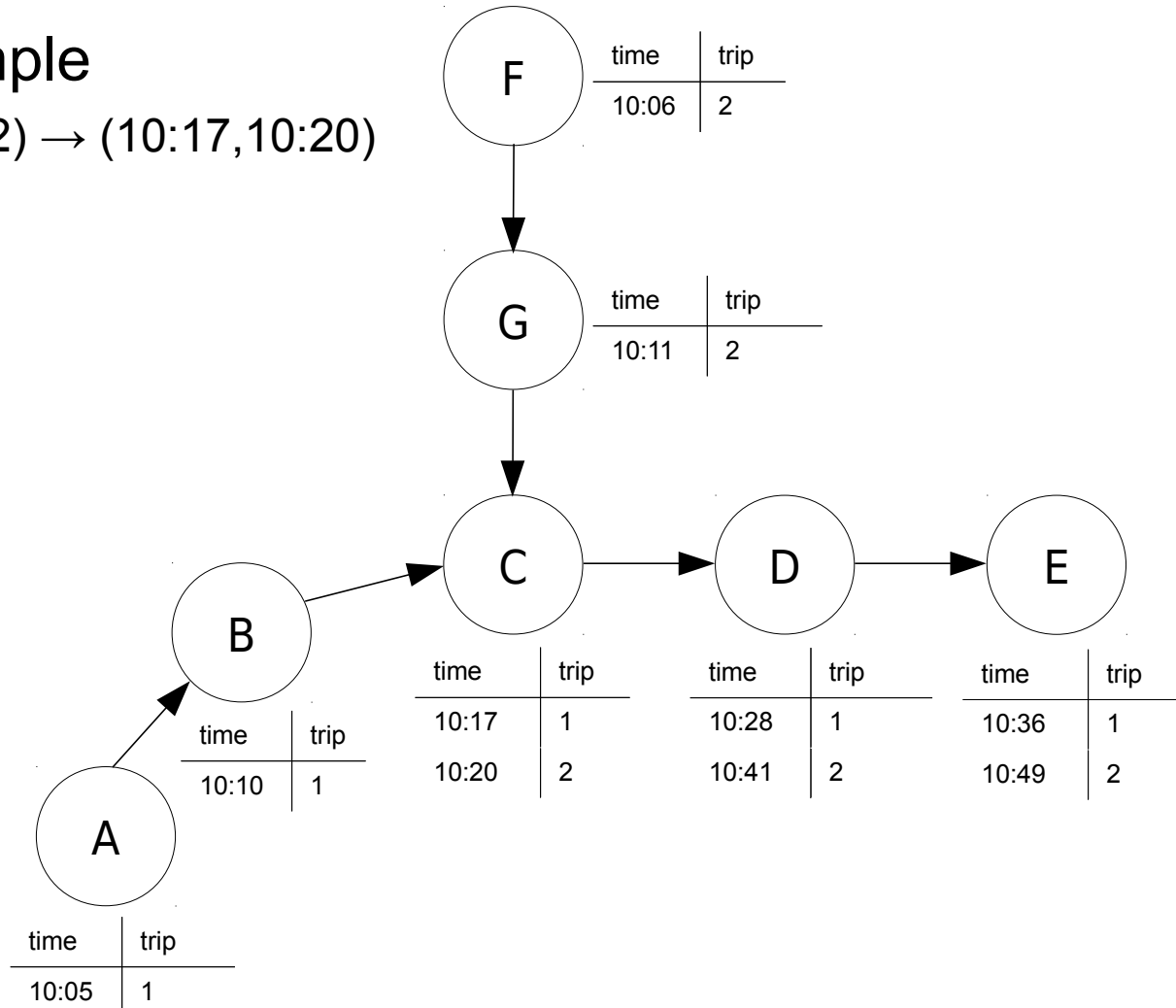


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- Example

- $(1,2) \rightarrow (10:17,10:20)$



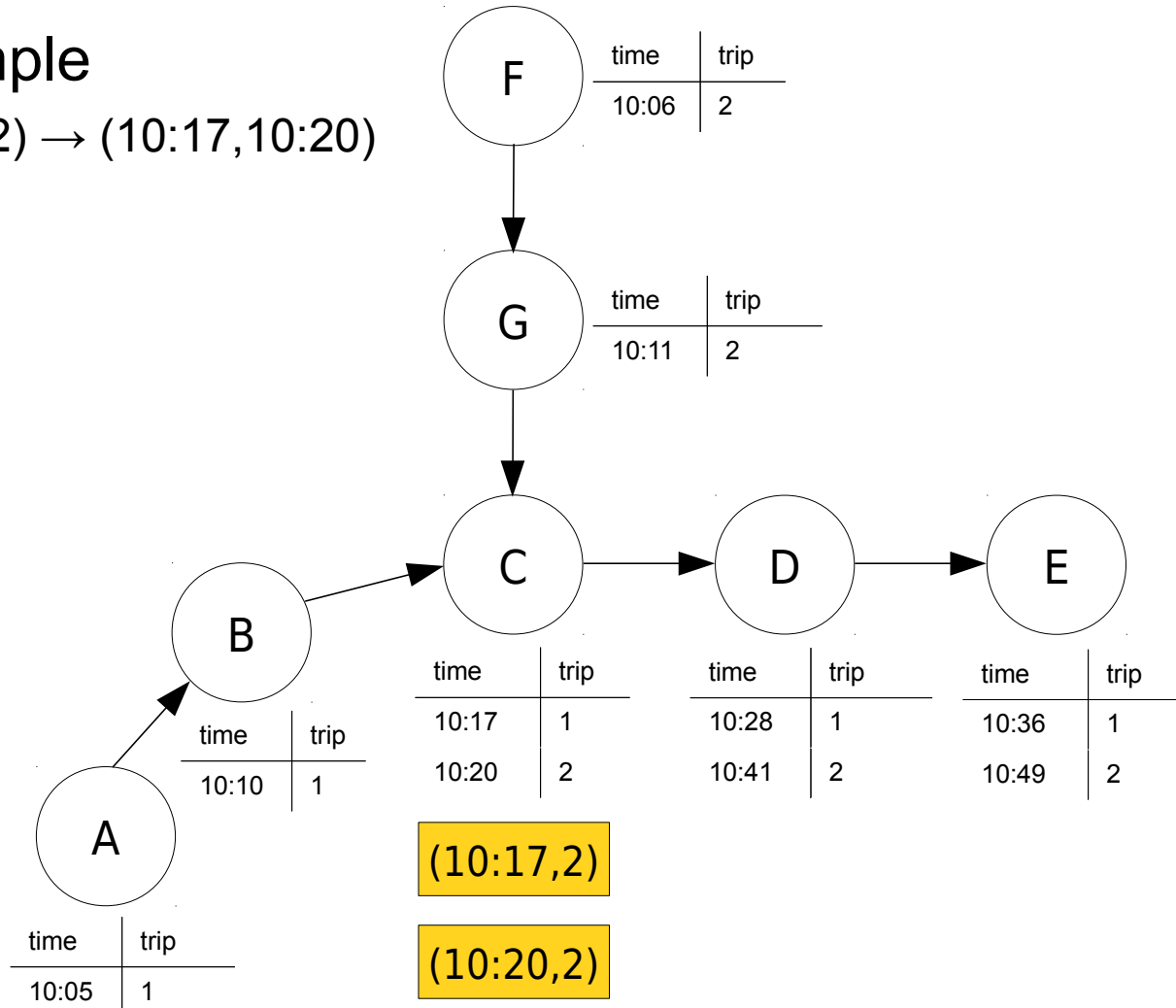


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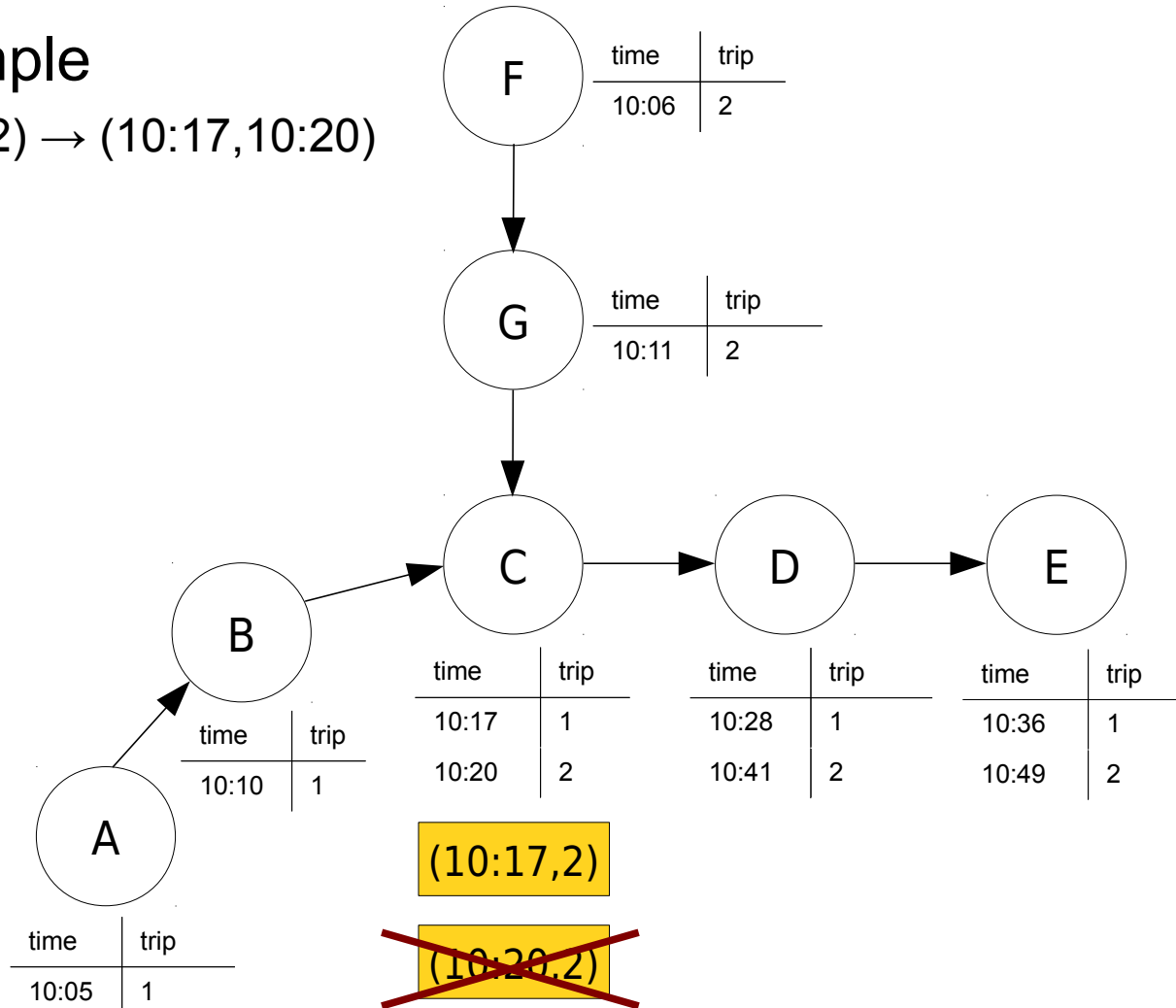


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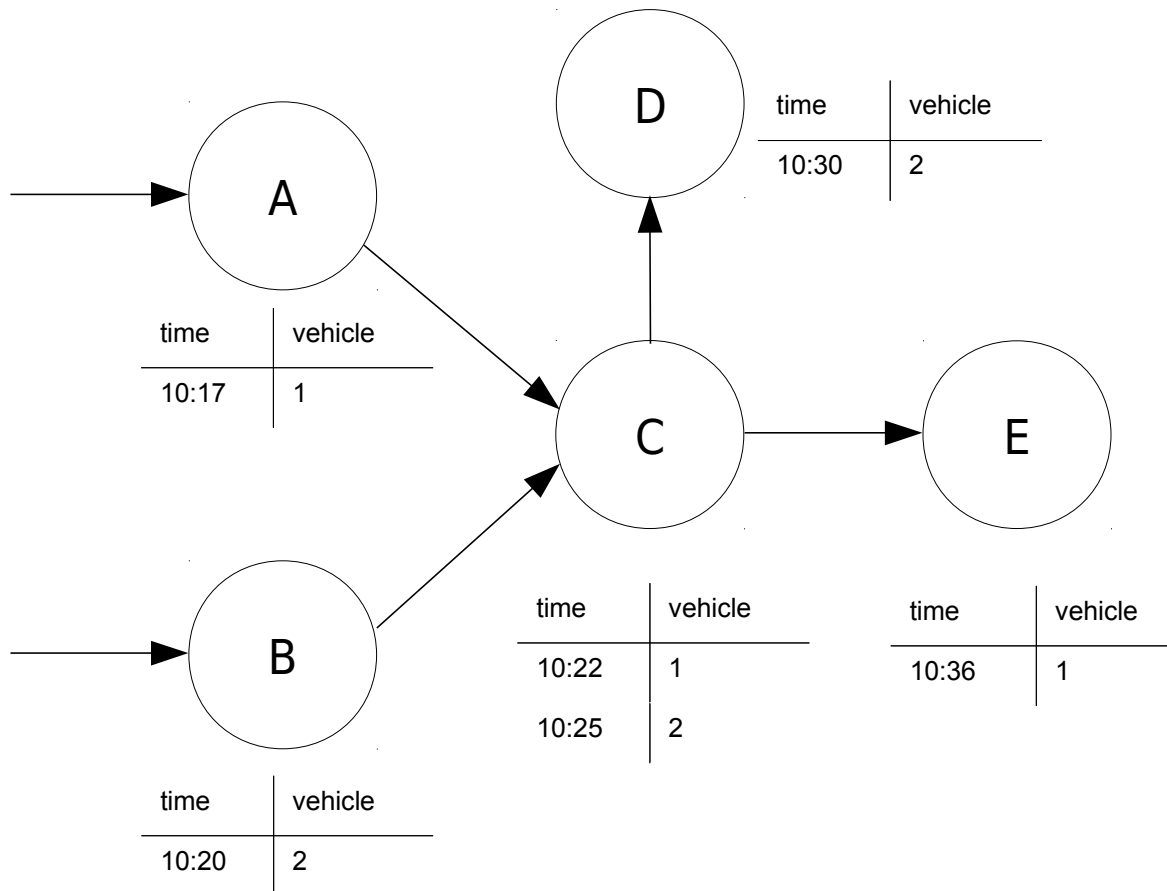


- Time-Expanded Approach
  - $(t, p) \leq (t', p')$  if and only if  $t \leq t'$  and  $p \leq p'$
  - $(t, p) < (t', p')$  if and only if  $(t < t' \wedge p \leq p') \vee (t \leq t' \wedge p < p')$
  - $(t, p)$   $(t', p')$  incomparable if neither  $(t, p) \leq (t', p')$  nor  $(t', p') \leq (t, p)$
- Time-Dependent Approach
  - for labels  $(t, p)$  and  $(t', p')$  with  $\ell = \ell'$  use label domination in the time expanded sense
  - $(t, p) < (t', p')$  if and only if  $t + TB \leq t' \wedge p < p'$
  - $(t, p)$   $(t', p')$  incomparable if neither  $(t, p) < (t', p')$  nor  $(t', p') < (t, p)$

# Time Dependent Problem 1



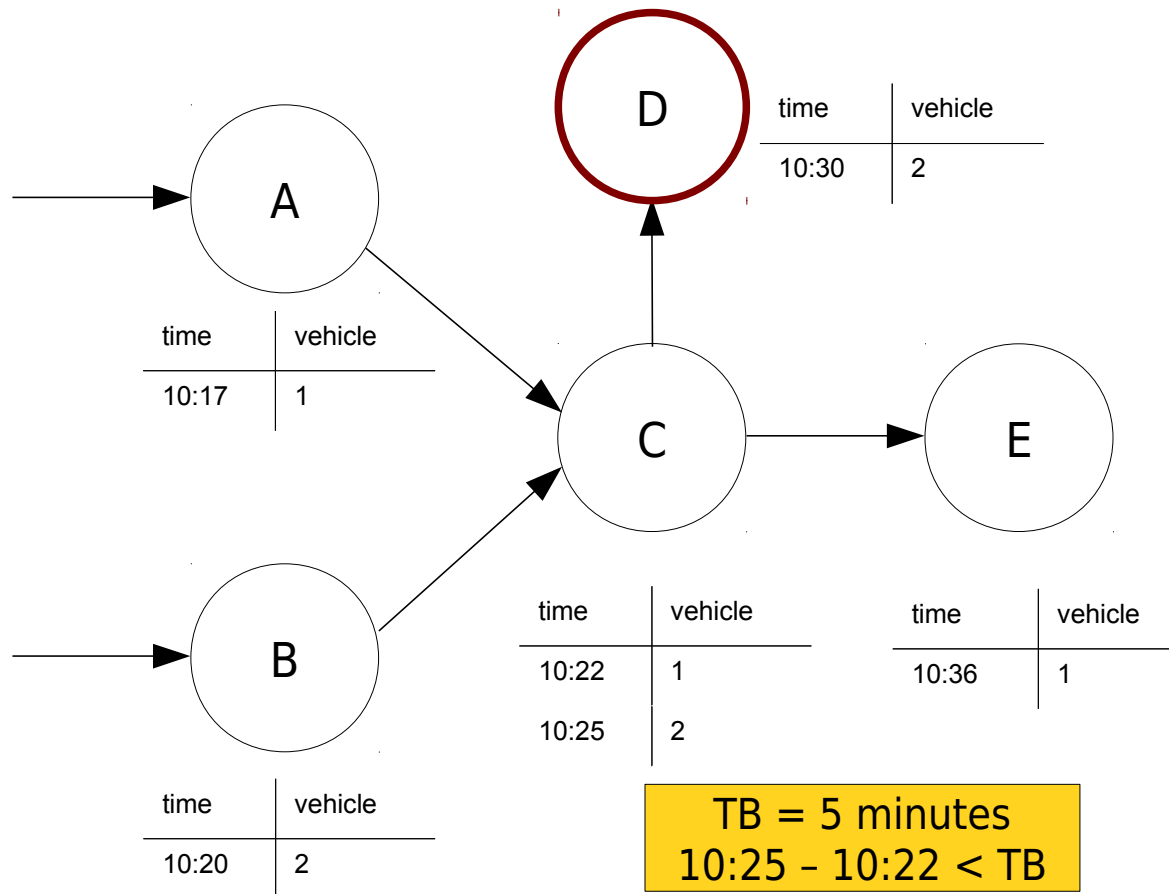
- Keeps labels with times  $t$  and  $t'$  with  $|t-t'| < TB$



# Time Dependent Problem 1



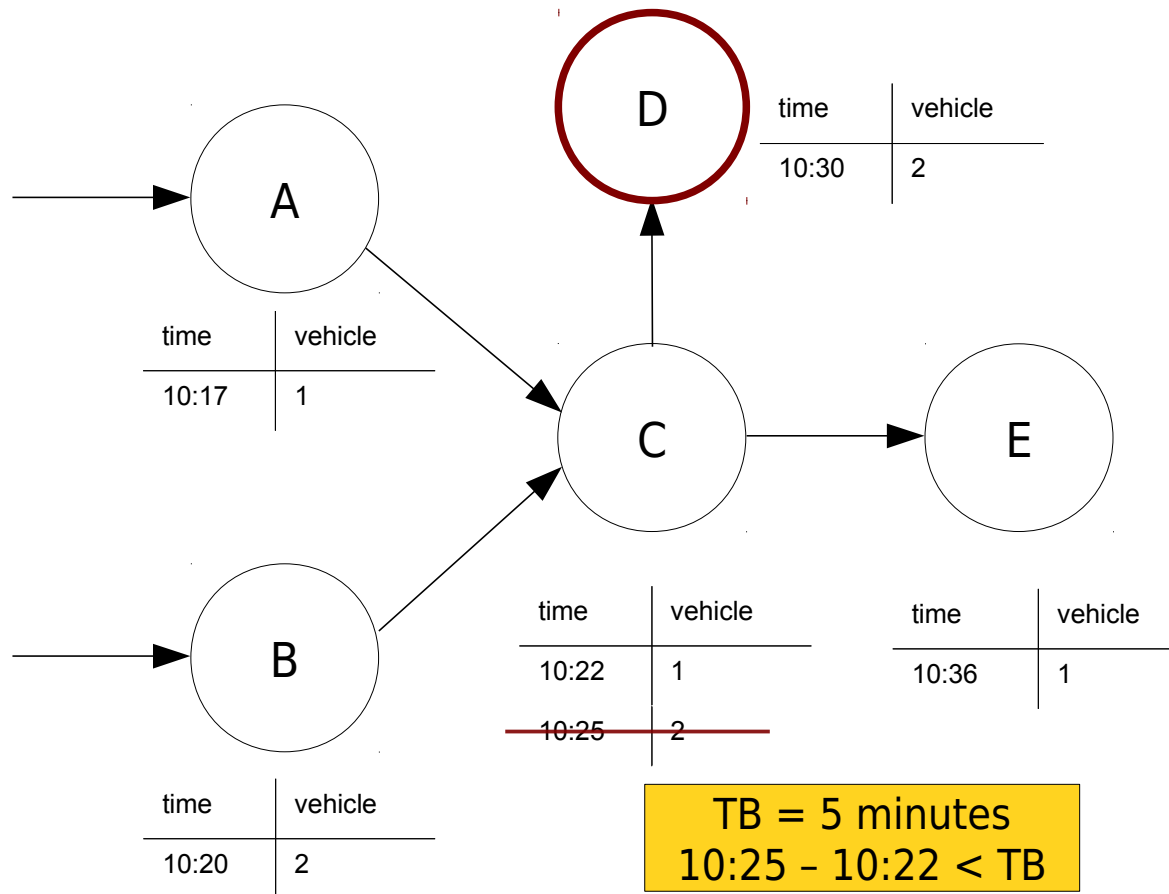
- Keeps labels with times  $t$  and  $t'$  with  $|t-t'| < TB$



# Time Dependent Problem 1



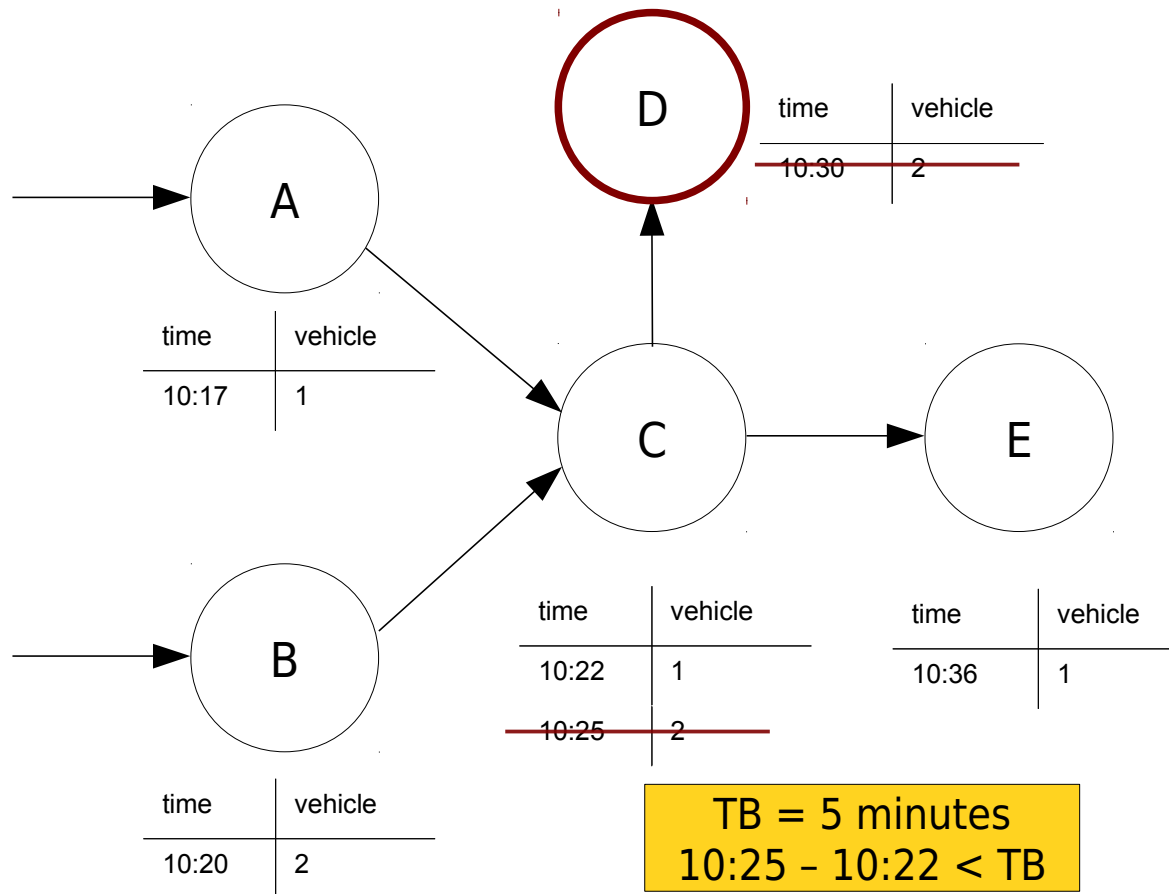
- Keeps labels with times  $t$  and  $t'$  with  $|t-t'| < TB$



# Time Dependent Problem 1



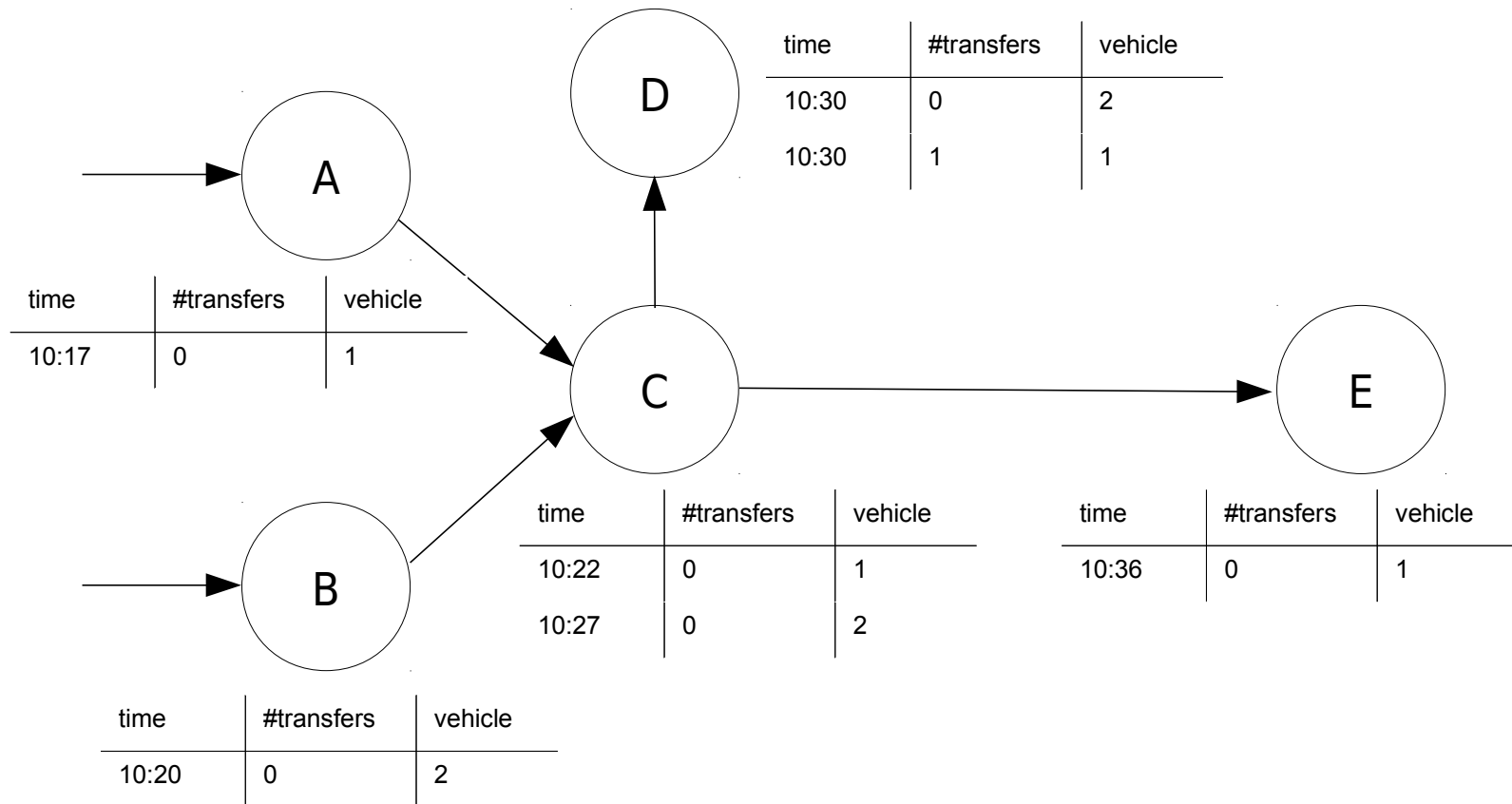
- Keeps labels with times  $t$  and  $t'$  with  $|t-t'| < TB$



# Time-Dependent Problem 2



- Keeps labels where  $p = p'$

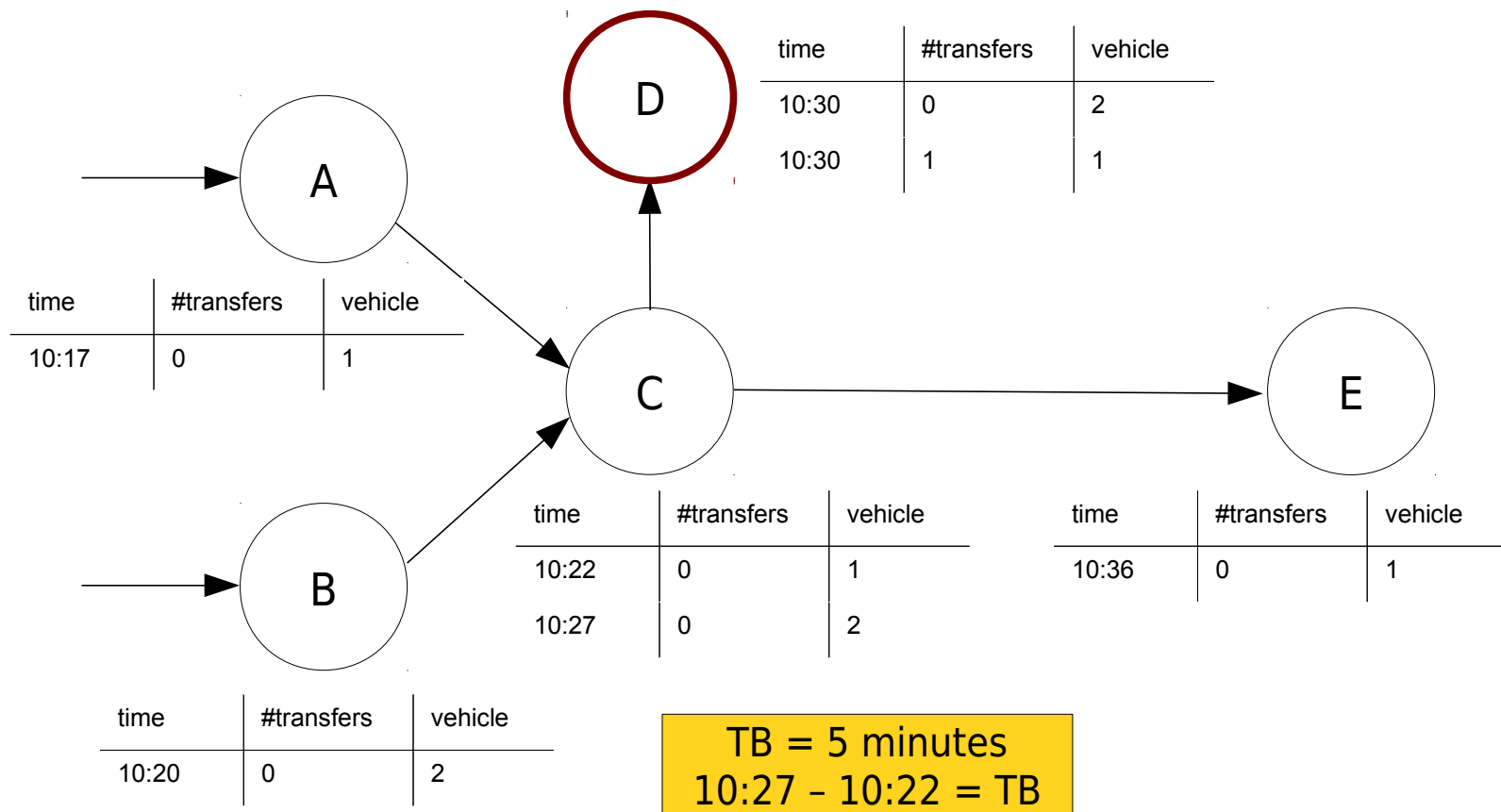




# Time-Dependent Problem 2



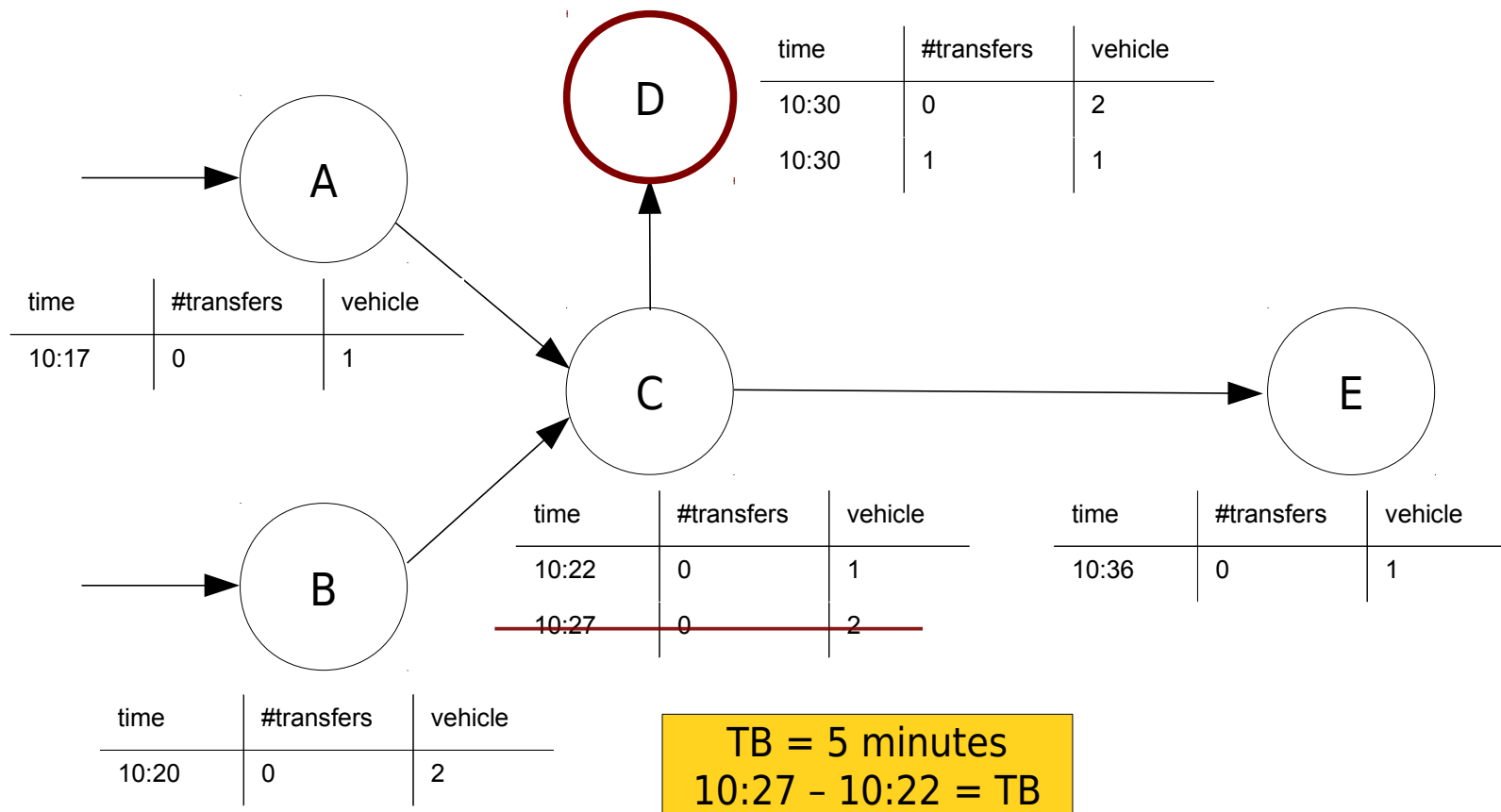
- Keeps labels where  $p = p'$



# Time-Dependent Problem 2



- Keeps labels where  $p = p'$



# Time-Dependent Problem 2



- Keeps labels where  $p = p'$

