# Evaluation of Investment Strategies for Cryptocurrencies 

How to get Rich Quick with this one Weird Trick (?)

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(1) The Problem: Investing in Bitcoin for Fun and Profit
(2) The Solution: Deploy a Trading Bot using a popular Trading Strategy
(3) The Evaluation: Are we rich yet?

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## Introduction

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- Buy
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Objective: Maximum profit

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ROI Return on Investment:
Percentage of funds gained/lost

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- Buy 2 BTC for $100 \$$ each


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\Rightarrow \mathrm{ROI}=\frac{\frac{F_{b}}{p_{b}} p_{s}-F_{b}}{F_{b}}=\frac{p_{s}}{p_{b}}-1
\end{aligned}
$$

## Formal Problem Definition

Given:

- Current point in time $t$
- Prices $p=p_{0}, p_{1}, p_{2}, \ldots, p_{t}$
- Trades $T=\left\{\left(b_{1}, s_{1}\right),\left(b_{2}, s_{2}\right), \ldots\right\}$


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The strategy which generated $T$ is called optimal, if there exists no set $T^{\prime}$, such that:

$$
\left(\prod_{(b, s) \in T} \frac{p_{s}}{p_{b}}\right)-1<\left(\prod_{\left(b^{\prime}, s^{\prime}\right) \in T^{\prime}} \frac{p_{s^{\prime}}}{p_{b^{\prime}}}\right)-1
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(Without cost)

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The strategy which generated $T$ is called optimal, if there exists no set $T^{\prime}$, such that:

$$
\left(\prod_{(b, s) \in T} \frac{p_{s} \cdot(1-c)}{p_{b} \cdot(1+c)}\right)-1<\left(\prod_{\left(b^{\prime}, s^{\prime}\right) \in T^{\prime}} \frac{p_{s^{\prime}} \cdot(1-c)}{p_{b^{\prime}} \cdot(1+c)}\right)-1
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\quad \text { (With cost) } \\
\text { Why the brackets? }
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## Can we do better?

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## The Basic Idea

- Deploy a bot that can buy/sell when signal is given
- The signal is produced by another popular strategy:

The SMAC

## The SMA: Simple Moving Average

- For each data point, calculate the average of last n data points


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Figure: Black line: Price over Time, Blue Line: SMA with a window of 10

## The SMA

Formula for SMA $s_{t}$ with window $n$ :

$$
s_{t}=\frac{1}{n} \cdot \sum_{i=0}^{n-1} p_{t-i}
$$

## The SMAC Strategy

SMAC Simple Moving Average Crossover

- For each data point, calculate two SMAs with different windows
- If the difference between the SMAs changes sign, buy/sell


## The SMAC Strategy: Example



Figure: Red SMA window: 6, Blue SMA window: 10

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Sell signal


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## The SMAC Strategy

- Let the window values be $m, n$ with $m<n$
- Fast SMA: $f_{t}=\frac{1}{m} \cdot \sum_{i=0}^{m-1} p_{t-i}$
- Slow SMA: $s_{t}=\frac{1}{n} \cdot \sum_{i=0}^{n-1} p_{t-i}$
- Difference: $d_{t}=f_{t}-s_{t}$
- Strategy:

$$
\begin{aligned}
& d_{t-1}<0 \text { and } d_{t} \geq 0 \Rightarrow \text { Buy } \\
& d_{t-1}>0 \text { and } d_{t} \leq 0 \Rightarrow \text { Sell }
\end{aligned}
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## Theory: An Optimal Model

- Assume price decreases linearly $p_{t}=p_{0}-t \cdot k$


Figure: $k=5$, Red SMA window: 2, Blue SMA window: 4

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$\geq k\left(\frac{n \cdot m}{2}-1\right)$


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- Here: change $\leq-k\left(\frac{n \cdot m}{2}-1\right)$


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## Theory: An Optimal Model

 And so on...

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## Bitcoins Next Top Model?

- $p_{0} \geq \frac{n \cdot m}{2} \cdot k$
- ROI: $\frac{p_{0}}{p_{0}-k}-1$
- Length: $n \cdot m+2$


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- $p_{0}=50 \geq 20$


Figure: $k=5, m=2, n=4$

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\frac{50}{50-5}-1=+11.1111 \%
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- Length: $2 \cdot 4+2=10$
- Seems reasonable


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- For a realistic setting: $k=5, m=50, n=100$ :
- $p_{0} \geq 12500$


Figure: $k=5, m=50, n=100$

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- Length:

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50 \cdot 100+2=5002
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Figure: $k=5, m=50, n=100$

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- $p_{0} \geq 12500$
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- Length:
$50 \cdot 100+2=5002$
- Does not seem reasonable


Figure: $k=5, m=50, n=100$

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- And if it is the SMAC: For what window setting?


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Optional: Formal definition of the binomial test setting

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- 10, 20, 50, 100, 200 ( 10 different settings in total)
- Settings used by R+V Insurance (Volksbank):
- 38, 200
- Total number of recommended settings:
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- What gives a higher chance of success:

Choosing a recommended setting or one at random?

## Test Results

## Dataset

Recommended settings (11) All settings (44850)

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Bitcoin (daily)

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| Bitcoin (daily) | 0 | $0.033 \%(15)$ |
| :--- | :--- | :---: |
| Bitcoin (4-hourly) | 0 | 0 |

## Test Results

## Dataset

Bitcoin (daily)
Bitcoin (4-hourly)
Ethereum

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45.45\% (5)

0
27.77\% (12454)

## Test Results

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Bitcoin (daily)
Bitcoin (4-hourly)
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| Bitcoin (daily) | 0 | $0.033 \%(15)$ |
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| Bitcoin (4-hourly) | 0 | 0 |
| Ethereum | $45.45 \%(5)$ | $27.77 \%(12454)$ |
| Dow Jones | 0 | $0.68 \%(307)$ |

## Test Results

## Dataset

Bitcoin (daily)
Bitcoin (4-hourly)
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Microsoft

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The recommended settings do not give a higher chance for profit!

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Day trading strategies are basically astrology for Millenials

## Thank you!

## Cost

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## Cost

- How do cryptocurrency exchanges earn money?
- With the spread
- Spread: Difference between buying and selling price
- Example, where spread is $2 \%$ :
- "Regular" BTC price is $100 \$$
- Exchange will sell BTC for 101\$
- Exchange will buy BTC for $99 \$$
- Note: This is more complex in a real setting
- (Based on price movement, amount of customers, trading volume, etc.)


## Compounded ROI

- For $T=\left\{\left(b_{1}, s_{1}\right), \ldots,\left(b_{n}, s_{n}\right)\right\}$


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$\bullet \Rightarrow \mathrm{ROI}=\left(F_{b_{1}} \cdot \prod_{i=1}^{n} \frac{p_{s_{i}}}{p_{b_{i}}}-F_{b_{1}}\right) \cdot \frac{1}{F_{b_{1}}}$


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- Solving the recursion:
- $F_{s_{n}}=\left(\prod_{i=1}^{n} \frac{p_{s_{i}}}{p_{b_{i}}}\right) \cdot F_{b_{1}}$
- $\Rightarrow \mathrm{ROI}=\left(F_{b_{1}} \cdot \prod_{i=1}^{n} \frac{p_{s_{i}}}{p_{b_{i}}}-F_{b_{1}}\right) \cdot \frac{1}{F_{b_{1}}}$
- $=\left(\prod_{(b, s) \in T} \frac{p_{s}}{p_{b}}\right)-1$


## Number of SMAC strategies

- Example: For slow window of 4, there are 3 possible settings
- $(4,3),(4,2),(4,1)$


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\sum_{i=2}^{n} i-1=\sum_{i=1}^{n-1} i=\frac{n(n-1)}{2}
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- Then we get type II error probability $\beta=0.053$
- And power $(1-\beta)=0.947$


## Bitcoin Price Data



## Ethereum Price Data



## Dow Jones Price Data



## Microsoft Price Data



## EUR/USD Price Data



## Notes

